

# Soft R-Parity Violation

Yuhsin Tsai



in collaboration with **Gordan Krnjaic**



arXiv : 1304.7004

LANL , Sep 26, 2013

# The SUSY dilemma

The old belief :

SUSY solves the naturalness problem in a simple way

NATURAL & SIMPLE





# The SUSY dilemma

Now...

Experimental result forces us to choose either

NATURAL OR SIMPLE





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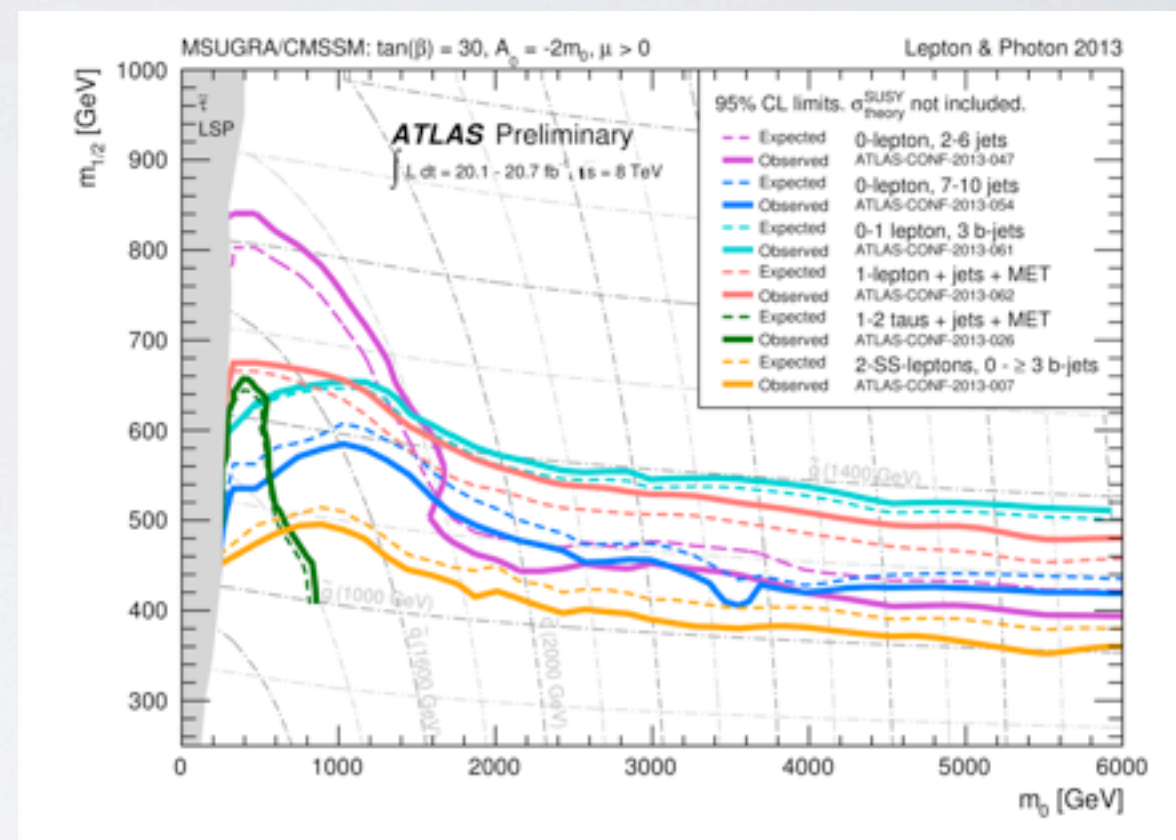
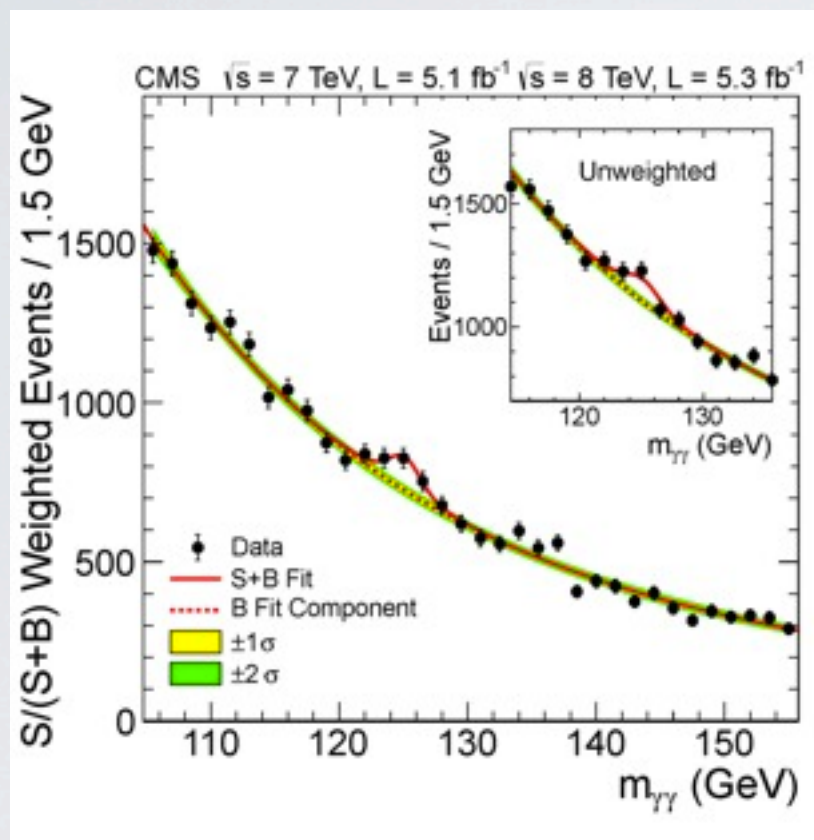
focus on natural SUSY in this talk



# The challenge on natural SUSY

126 GeV Higgs

bounds on the  $\tilde{t}$  &  $\tilde{g}$  masses



$$V \supset \frac{g^2}{8} (|H_u^0|^2 - |H_d^0|^2)^2$$

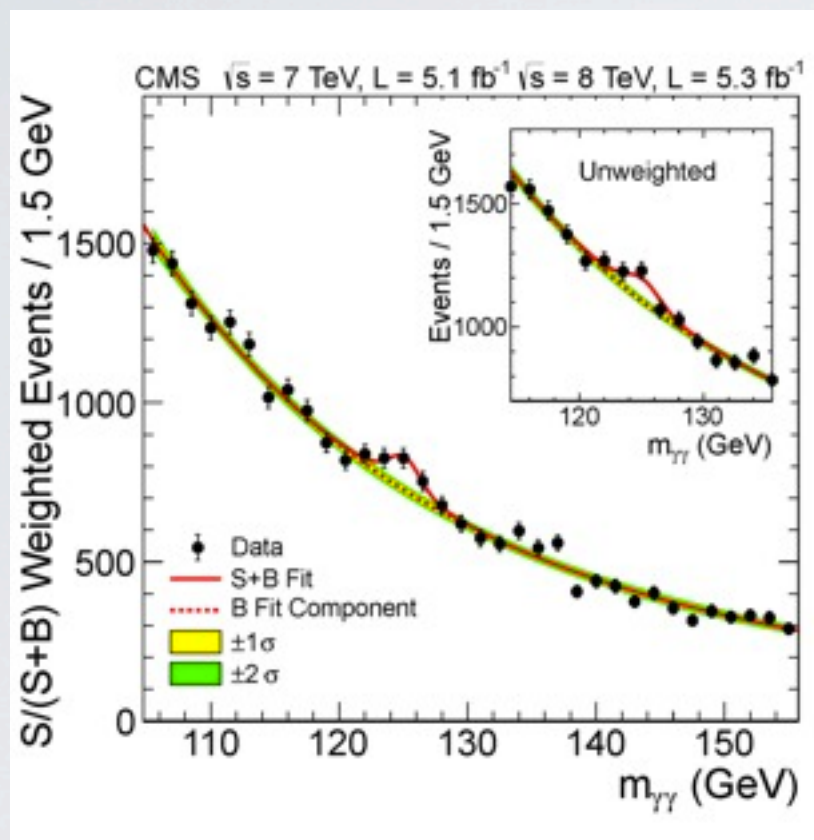
$$\Rightarrow m_h \simeq m_Z$$

from missing energy searches

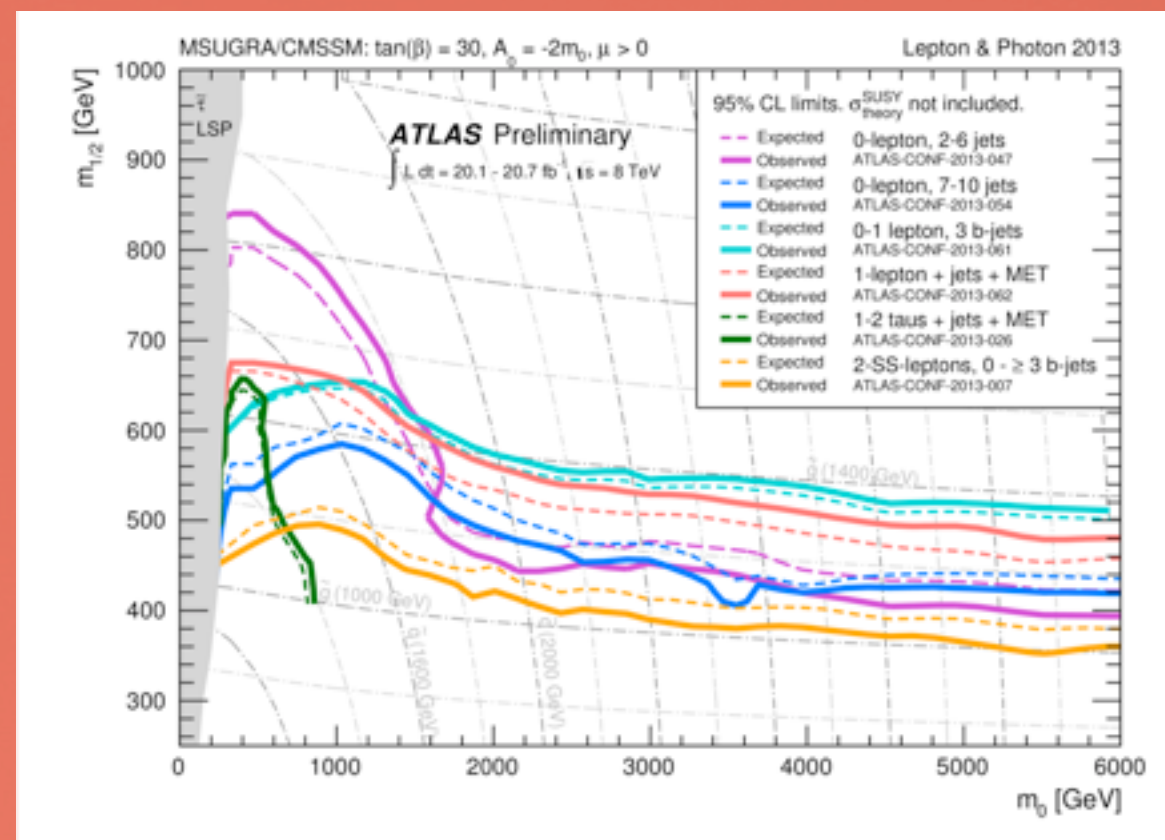


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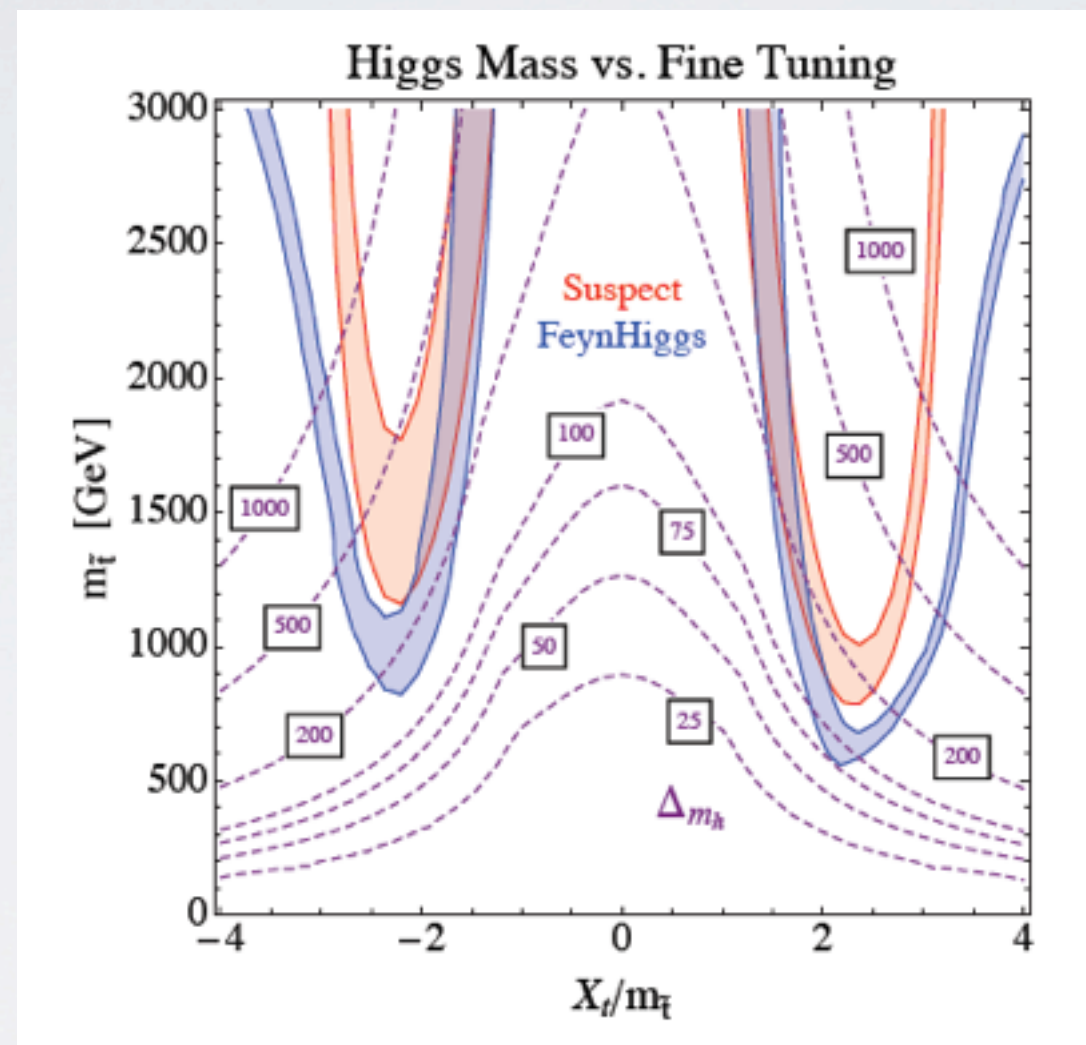


Try to relax bounds from direct searches



# The challenge on natural SUSY

The amount of tuning



Hall, Pinner and Ruderman  
(1112.2703)

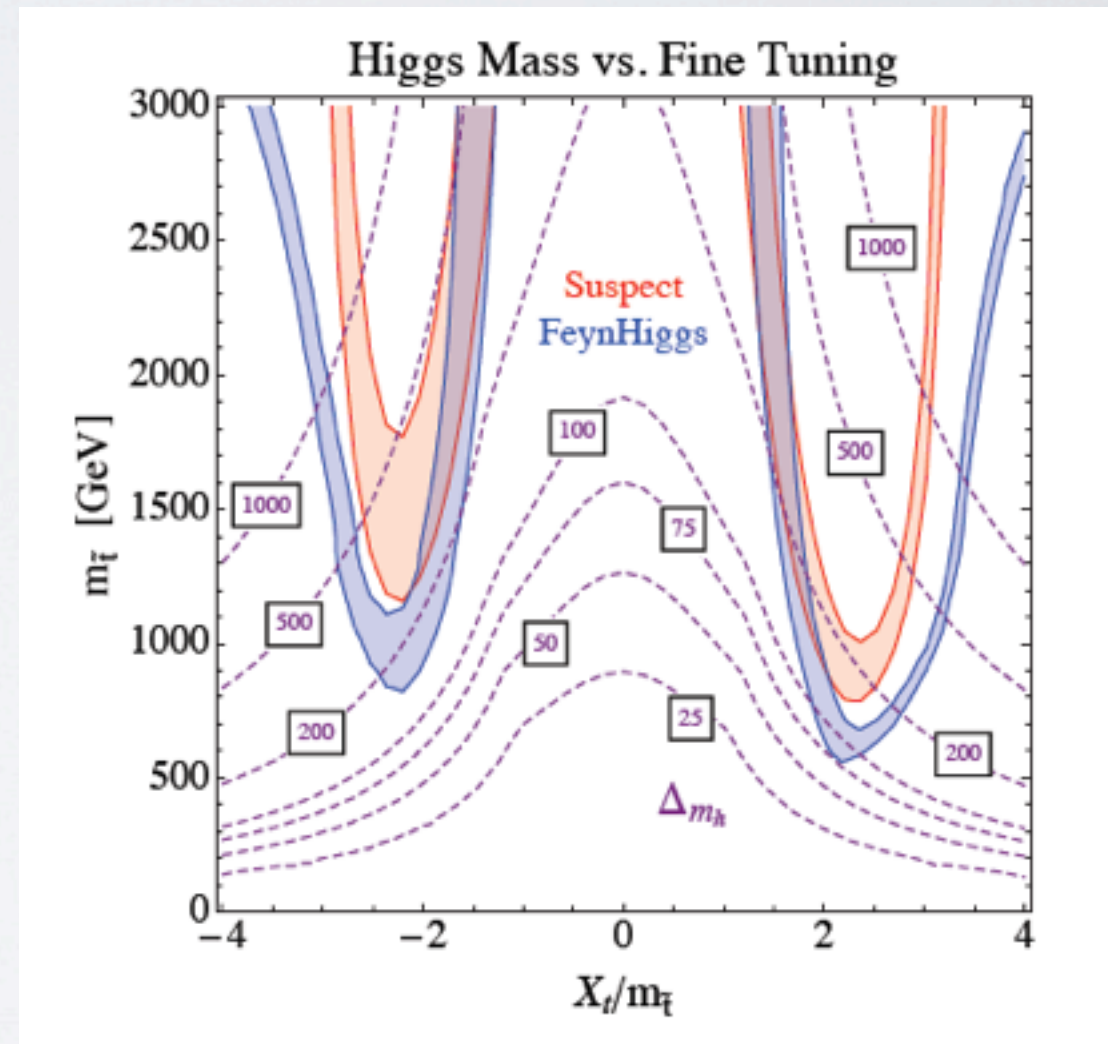


# Tuning from the stop & gluino

Two ways to relax the tuning :

change the radiative  
correction

change the collider  
constraint





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Example: Supersoft SUSY

$$\delta m_{H_u}^2 = -\frac{3 y_t^2}{8\pi^2} m_{\tilde{t}}^2 \log \frac{m_{\tilde{g}}^2}{m_{\tilde{t}}^2}$$

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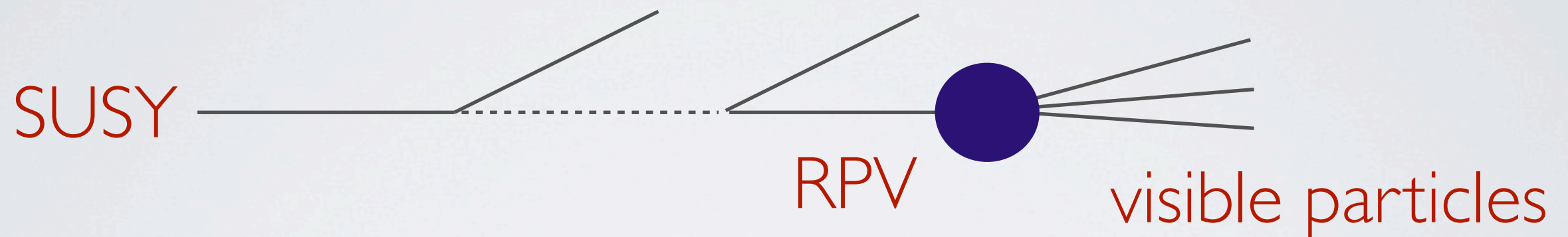
Example:

- compressed spectrum
- more cascade decays
- **R-parity violation**



# R-parity violation (RPV)

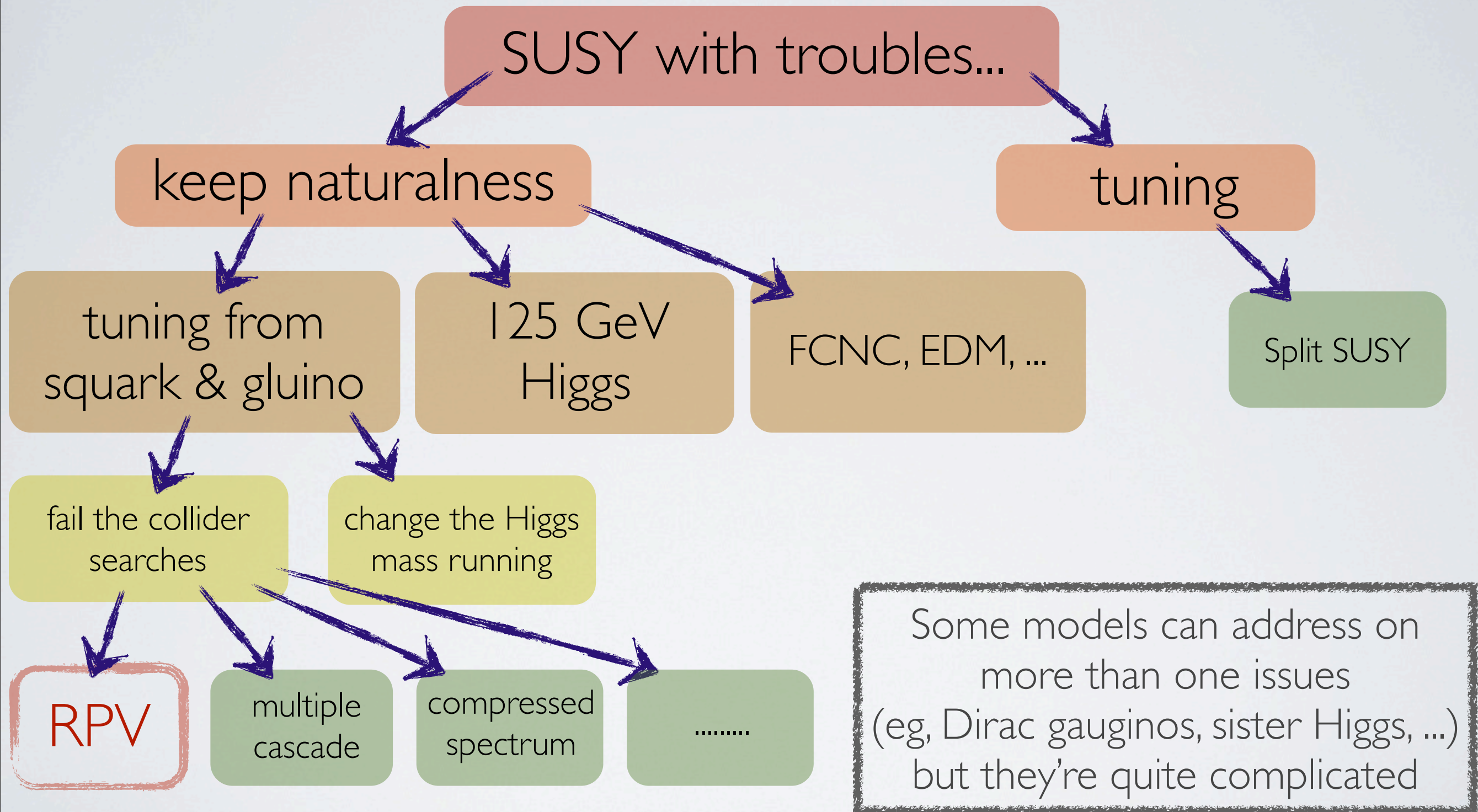
The LSP decay fails the MET searches



However, there are stringent flavor constraints!

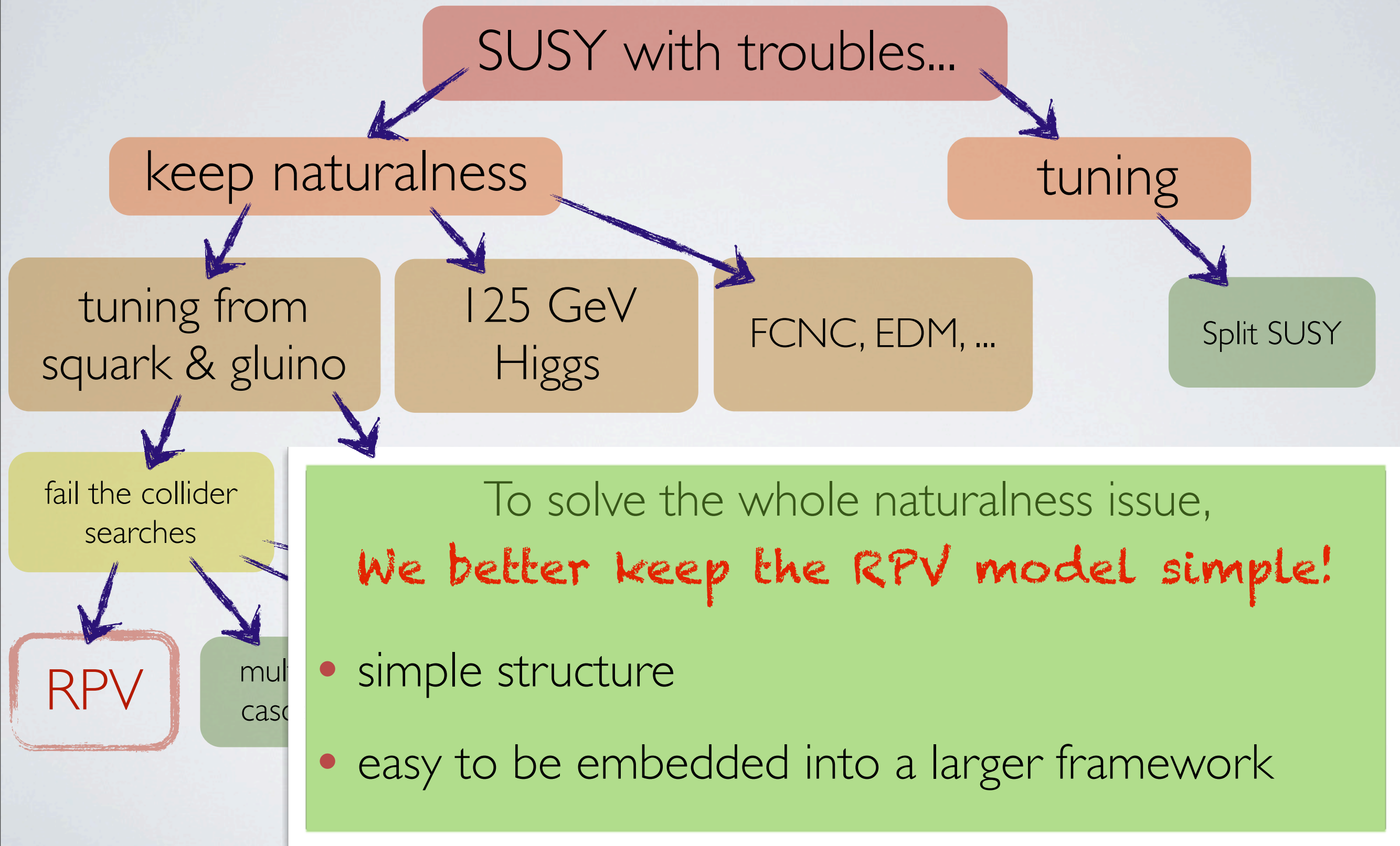
proton decay , neutron/anti-neutron oscillations ,  
di-nucleon decay , FCNC

# RPV in the natural forest





# RPV in the natural forest



# Models of R<sub>PV</sub>





# The RPV couplings

supersymmetric terms

$$W_{RPV} = \frac{\lambda_{ijk}}{2} L_i L_j \bar{E}_k + \lambda'_{ijk} Q_i L_j \bar{D}_k + \frac{\lambda''_{ijk}}{2} \bar{U}_i \bar{D}_j \bar{D}_k + \mu_{L_i} L_i H_u$$

soft breaking terms

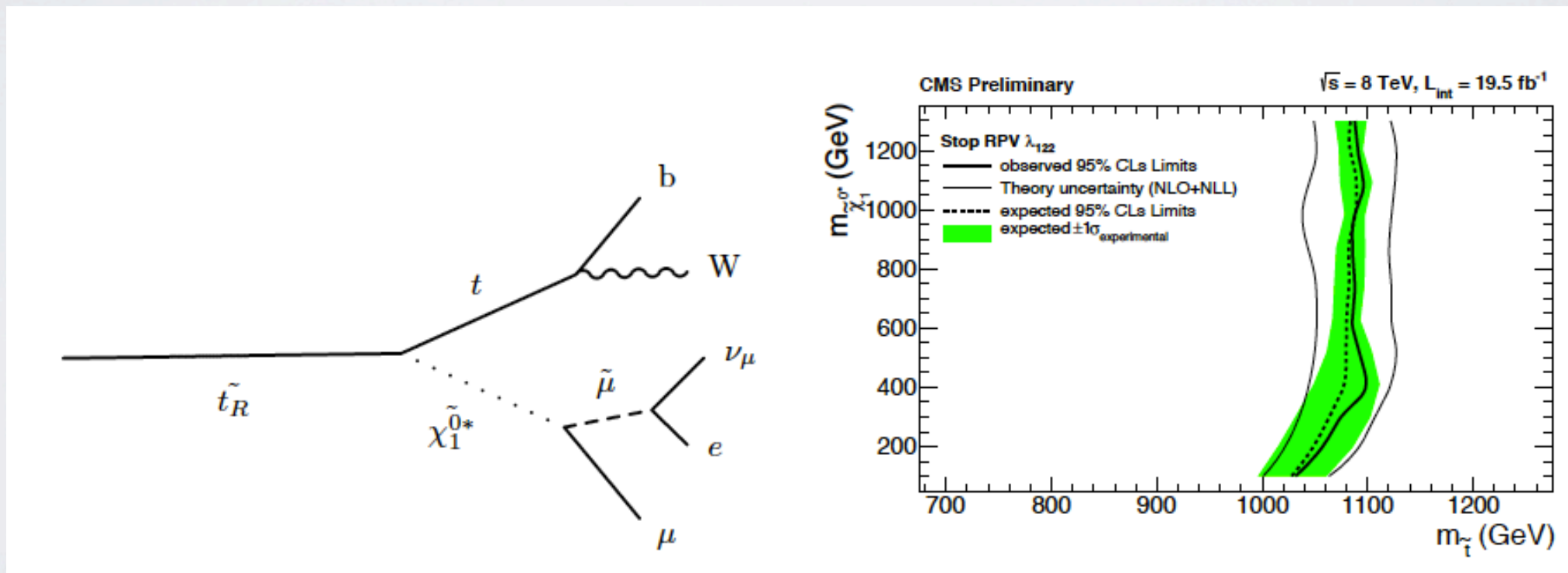
$$\mathcal{L}_{SUSY} \supset \frac{\mathcal{A}_{ijk}}{2} \tilde{L}_i \tilde{L}_j \tilde{\bar{E}}_k + \mathcal{A}'_{ijk} \tilde{Q}_i \tilde{L}_j \tilde{\bar{D}}_k + \frac{\mathcal{A}''_{ijk}}{2} \tilde{\bar{U}}_i \tilde{\bar{D}}_j \tilde{\bar{D}}_k + \mathcal{B}_i \tilde{L}_i H_u + h.c.$$

It's easier to have an RPV model  
that only violates B-number

# Leptonic RPV

$$W_{RPV} = \frac{\lambda_{ijk}}{2} L_i L_j \bar{E}_k + \lambda'_{ijk} Q_i L_j \bar{D}_k + \frac{\lambda''_{ijk}}{2} \bar{U}_i \bar{D}_j \bar{D}_k + \mu_{L_i} L_i H_u$$

$$\mathcal{L}_{SUSY} \supset \frac{\mathcal{A}_{ijk}}{2} \tilde{L}_i \tilde{L}_j \tilde{E}_k + \mathcal{A}'_{ijk} \tilde{Q}_i \tilde{L}_j \tilde{D}_k + \frac{\mathcal{A}''_{ijk}}{2} \tilde{U}_i \tilde{D}_j \tilde{D}_k + \mathcal{B}_i \tilde{L}_i H_u + h.c.$$



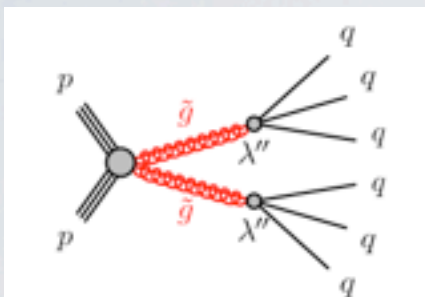
leptonic RPV is more constrained



# RPV through the baryon portal

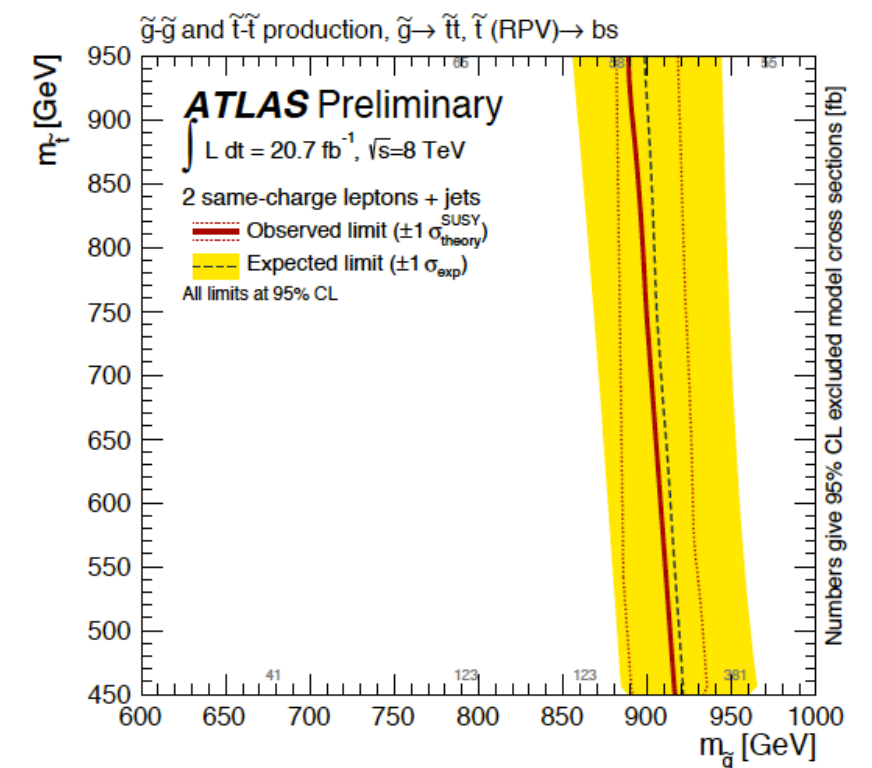
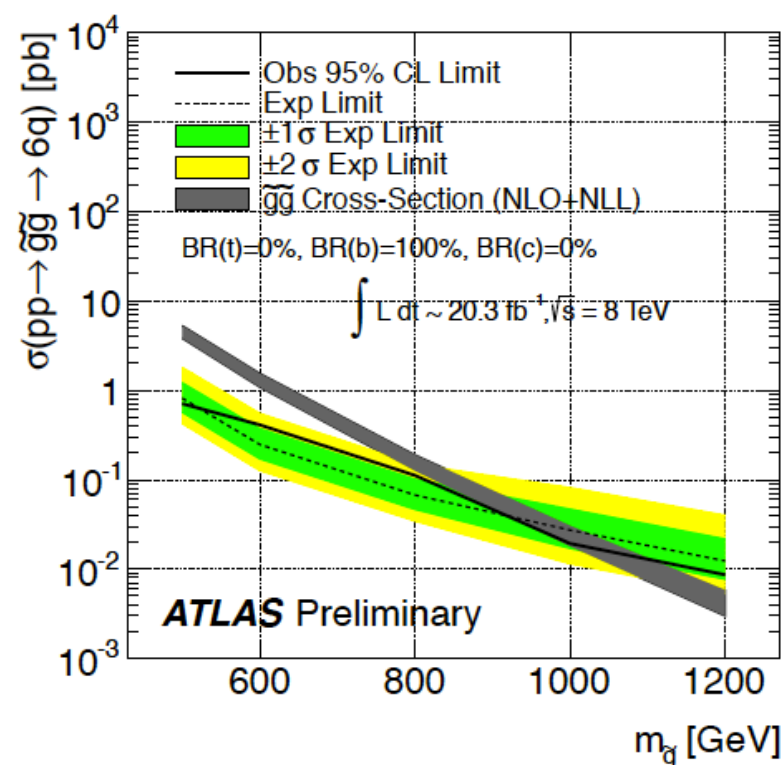
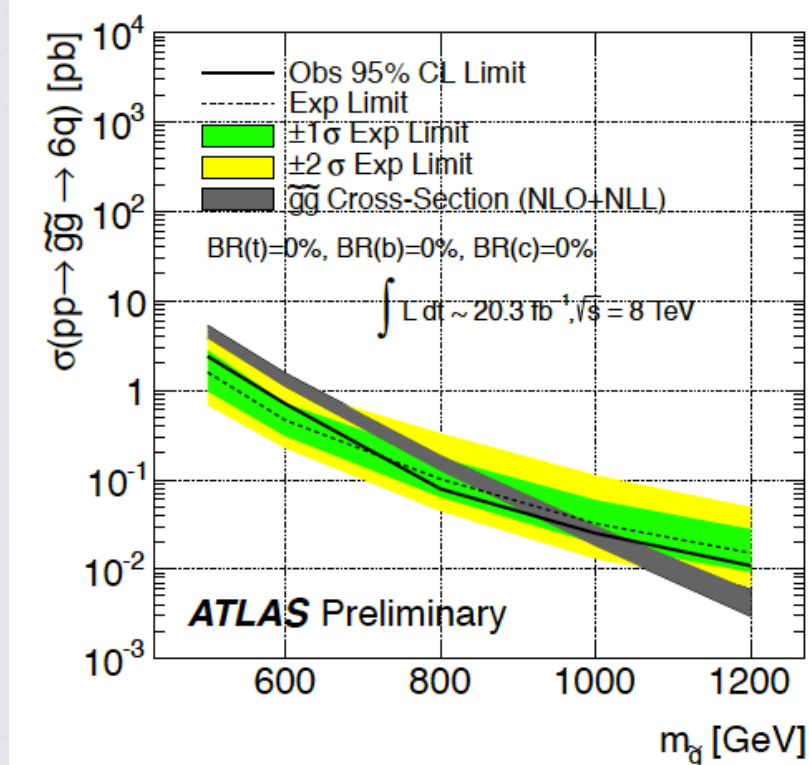
$$W \supset \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k$$

$$\mathcal{L} \supset \mathcal{A}''_{ijk} \tilde{U}_i \tilde{D}_j \tilde{D}_k$$



6-jet search

SSDL + b-jet



$$m_{\tilde{g}} > 900 \text{ GeV}$$

# Upper & lower bounds for $\lambda''_{u_i d_j d_k}$

With no L-number violation, we need  $\lambda''_{u_i d_j d_k} \leq 10^{-7}$  to satisfy flavor constraints (the statement depends on flavor structure)

Also, we need  $\lambda''_{u_i d_j d_k} \geq 10^{-7}$  for the squark decay to be prompt



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$$\lambda''_{u_i d_j d_k} \sim 10^{-7}$$

The rough size of baryonic RPV couplings

# Models with UDD

Example:

## Minimal Flavor Violation

Nikolidakis and Smith (0710.3129)

Csaki, Grossman and Heidenreich (1302.2146)

constrains all flavor violating processes with the appropriate Yukawa couplings, which also determine the size and scope of allowed RPV interactions.

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_B$	$U(1)_L$	$\mathbb{Z}_2^R$
$(QQQ)$	1	$\square\square\square$	1/2	1	0	—
$(QQ)Q$	8	$\square$	1/2	1	0	—
$(Y_u\bar{u})(Y_u\bar{u})(Y_d\bar{d})$	$8 \oplus 1$	1	-1	-1	0	—
$(Y_u\bar{u})(Y_d\bar{d})(Y_d\bar{d})$	$8 \oplus 1$	1	0	-1	0	—
$\det \bar{u}$	1	1	-2	-1	0	—
$\det \bar{d}$	1	1	1	-1	0	—
$QY_u\bar{u}$	$8 \oplus 1$	$\square$	-1/2	0	0	+
$QY_d\bar{d}$	$8 \oplus 1$	$\square$	1/2	0	0	+
$LY_e\bar{e}$	1	$\square$	1/2	0	0	+
$H_u$	1	$\square$	1/2	0	0	+
$H_d$	1	$\square$	-1/2	0	0	+

$$W \supset Y_{u_i} Y_{d_j} Y_{d_k} \bar{U}_i \bar{D}_j \bar{D}_k$$

The UV-completion can be challenging

Krnjaic and Stolarski (1212.4860)

Csaki and Heidenreich (1302.0004)



# General requirements

To obtain a small but non-zero  $\lambda''_{udd} \sim 10^{-7}$ , we need

- a symmetry that forbids the RPV couplings
- breaking of the symmetry
- some mediation that suppresses the  $\lambda''_{udd}$

There are many other things we want beside naturalness:

SUSY breaking, dark matter, Higgs mass, ...

Are we going to include different models for each of them?

# Soft RPV





## Question:

given a SUSY breaking model, what's the easiest way to embed a baryonic RPV in it?

# Soft RPV model

Generate RPV couplings through  
the SUSY breaking soft terms

## Motivations

embed RPV into a SUSY breaking setup,  
make the model more economic

another example: [dynamical RPV](#) by C. Csaki, E. Kuflik and T. Volansky (1309.5957)



# A SoftRPV model needs...

- a symmetry  $G$  that forbids the supersymmetric RPV couplings
- $G$ -breaking by SUSY breaking soft terms in a hidden sector
- mediation of the  $G$ -breaking effect to visible sector

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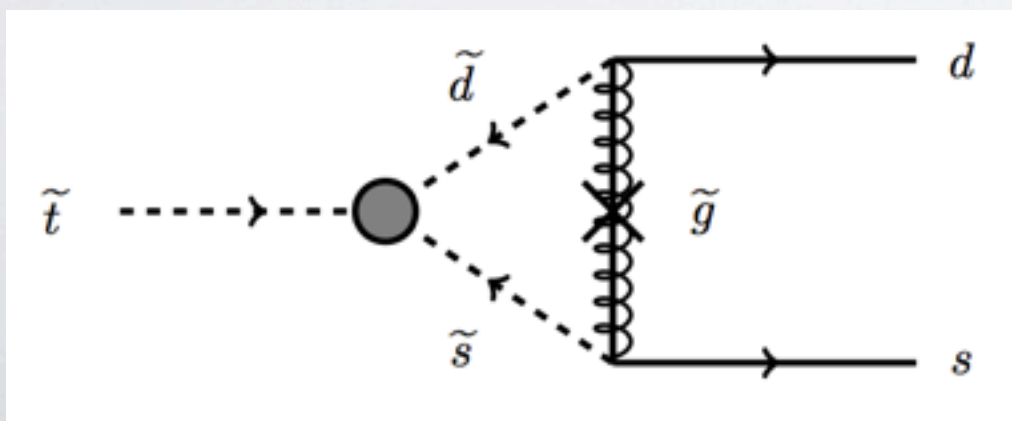
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$$A_{u_i d_j d_k} \tilde{U}_i \tilde{D}_j \tilde{D}_k$$



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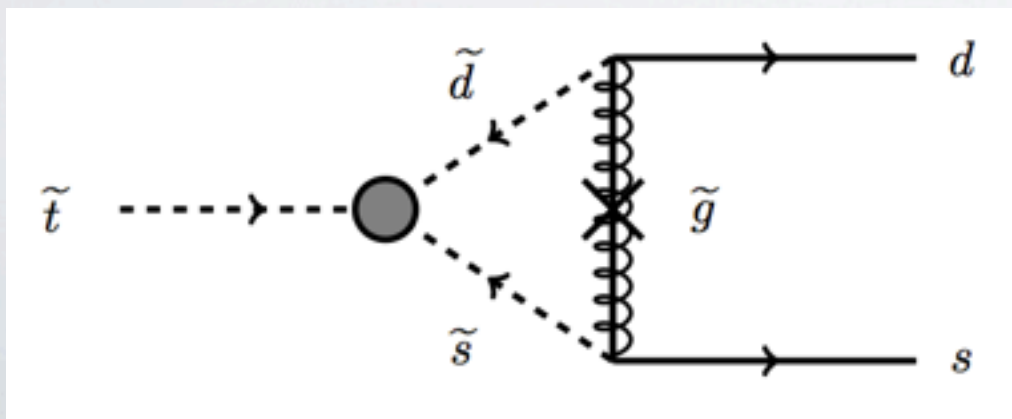
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$$\mathcal{A}_{u_i d_j d_k} \tilde{U}_i \tilde{D}_j \tilde{D}_k$$

Naively,  $\mathcal{A}_{u_i d_j d_k} \simeq \mathcal{A}_{soft}$

but  $\lambda''_{udd} \simeq \frac{g_s^2}{16\pi^2} \frac{\mathcal{A}_{soft}}{m_{\tilde{g}}} \simeq 10^{-2}$

forbidden by L- or B-violating constraints





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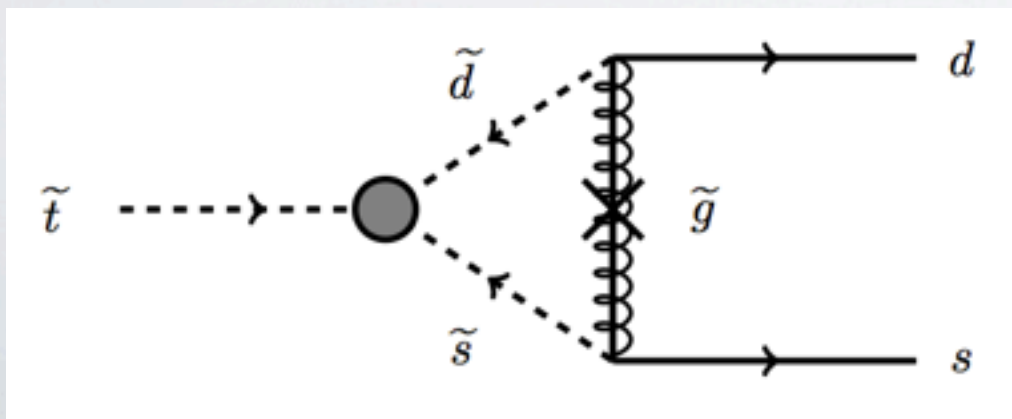
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# A Gauge-Mediation Example



# In this example

embed RPV in a GM setup

use R-symmetry to forbid the supersymmetric RPV terms

gravitino serves as a good dark matter candidate

no extra mass scales or small couplings need to be put in by hand

$$\lambda''_{udd} \sim \frac{g_s^2}{16 \pi^2} \frac{m_{soft}}{\sqrt{F}}$$

# To forbid the supersymmetric RPV

use the R-symmetry to forbid the RPV couplings

assign

$$R[Q, \bar{U}, \bar{D}] = 1, \quad R[L] = 4/3, \quad R[\bar{E}] = 2/3, \quad R[H_u, H_d] = 0$$

$$W_{RPV} = \frac{\lambda_{ijk}}{2} \cancel{L_i} \cancel{L_j} \bar{E}_k + \lambda'_{ijk} \cancel{Q_i} \cancel{L_j} \bar{D}_k + \frac{\lambda''_{ijk}}{2} \bar{U}_i \cancel{\bar{D}_j} \bar{D}_k + \mu_{I_i} \cancel{L_i} H_u$$

the fractional R-charges are used to  
forbid the generation of lepton-related operators



# Breaking & mediation

## Gauge mediation model

~~SUSY~~

$X \quad \Sigma \quad \bar{\Sigma}$

soft R-breaking sector

R-symmetry

$\bar{U} \quad \bar{D}$   
 $Q \quad L \quad \bar{E} \quad H_u \quad H_d$

visible sector

No RPV couplings

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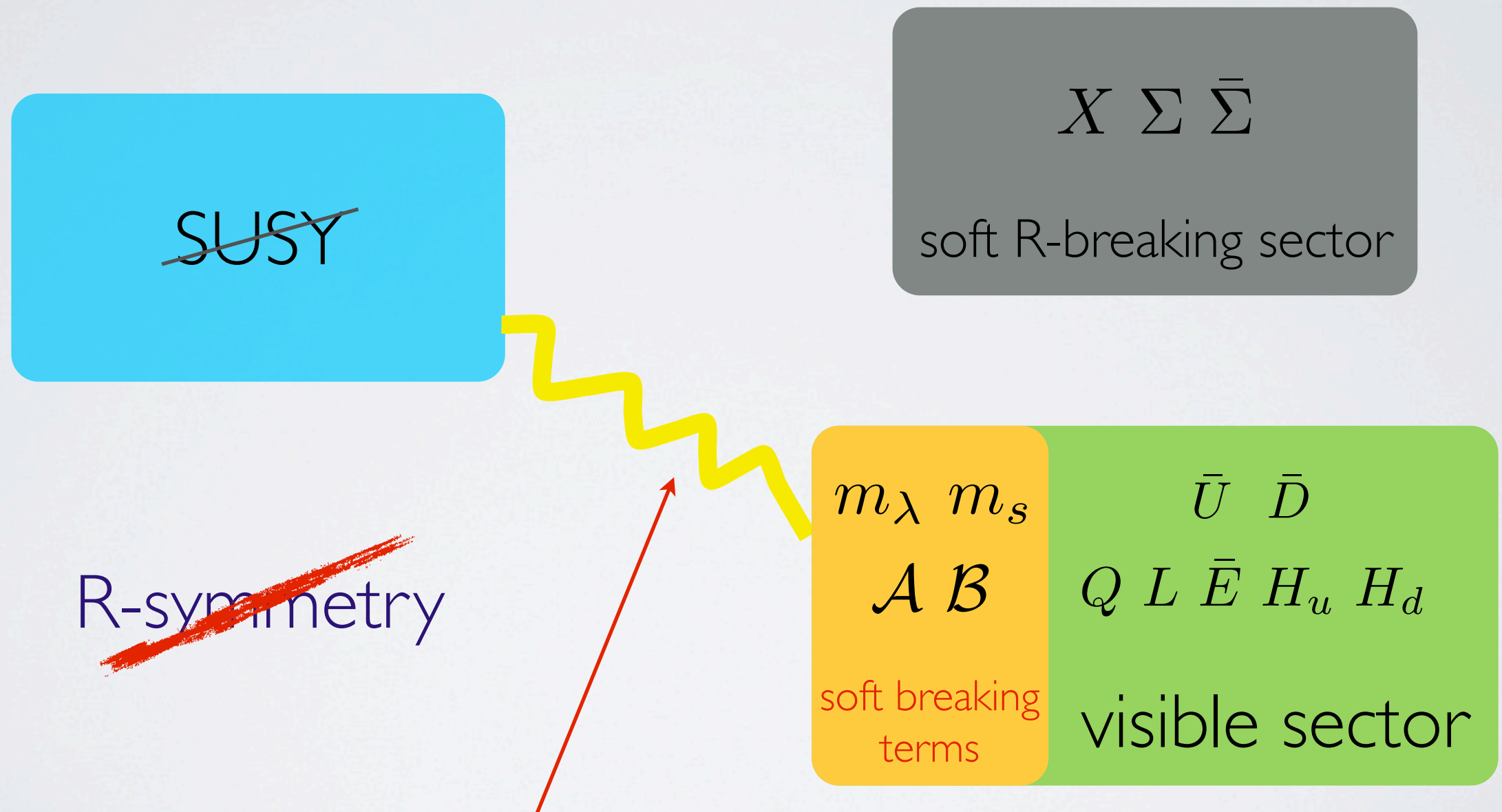
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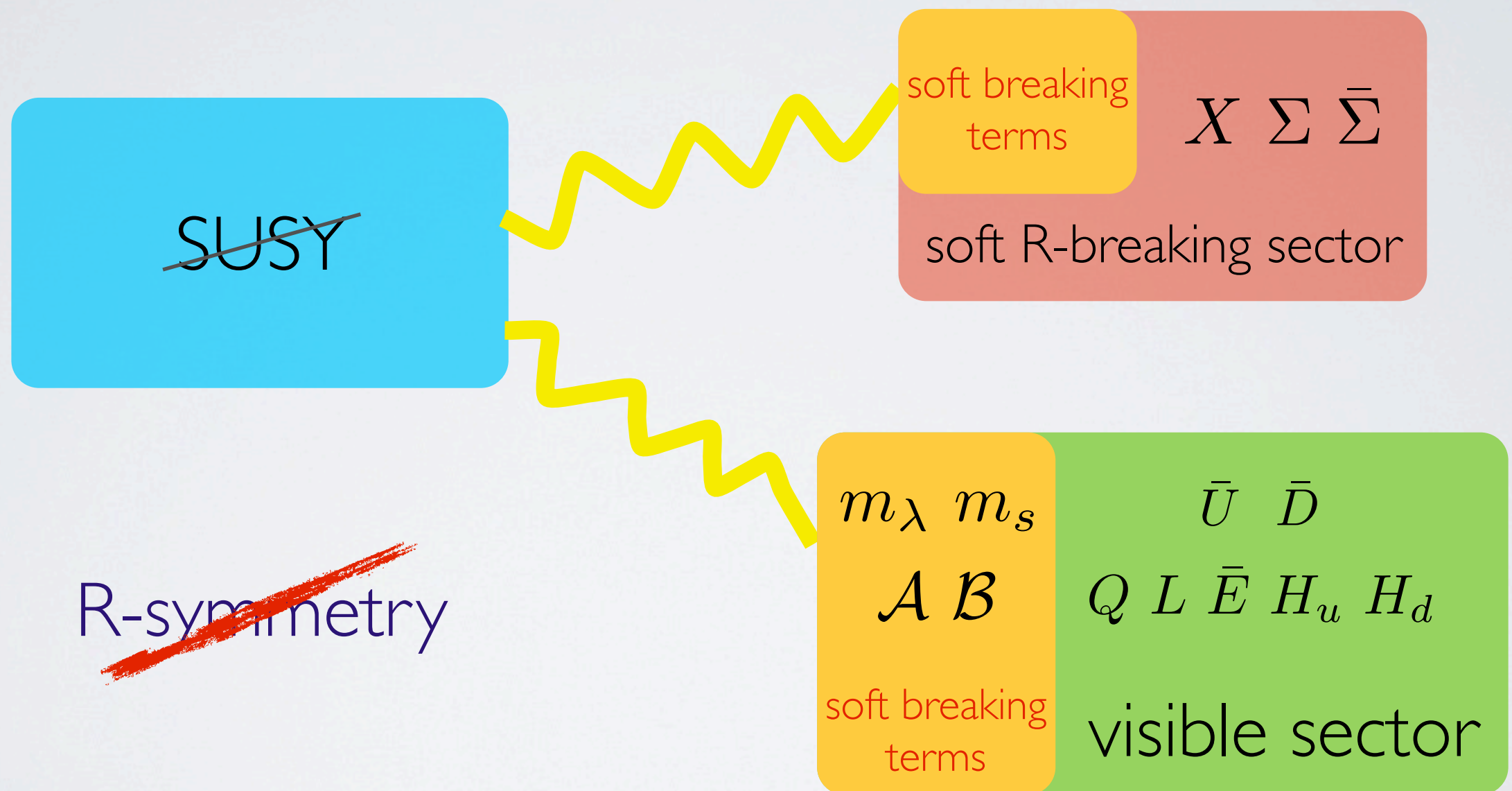


No B- or L-violation, still no RPV couplings



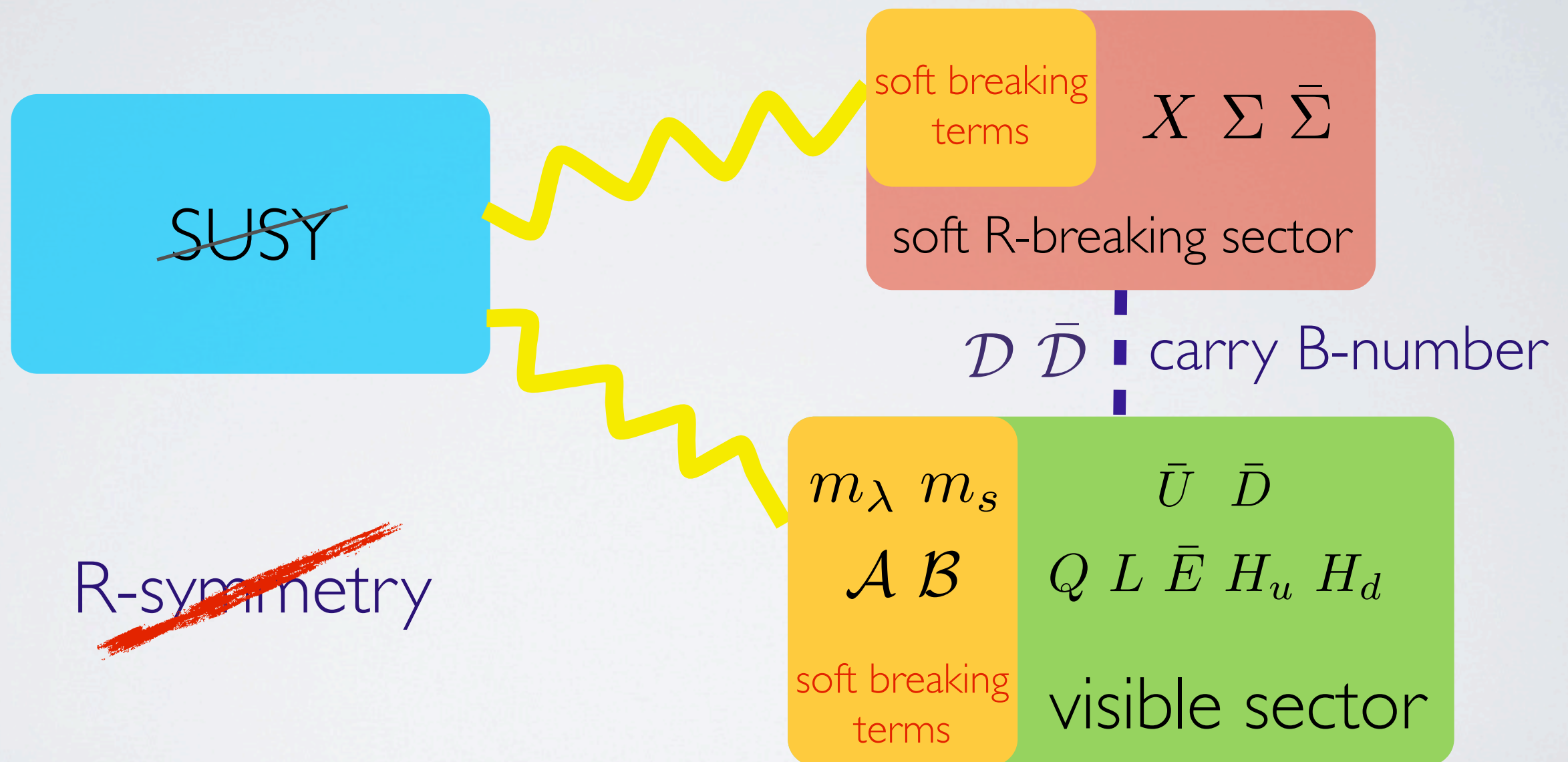
# Breaking & mediation

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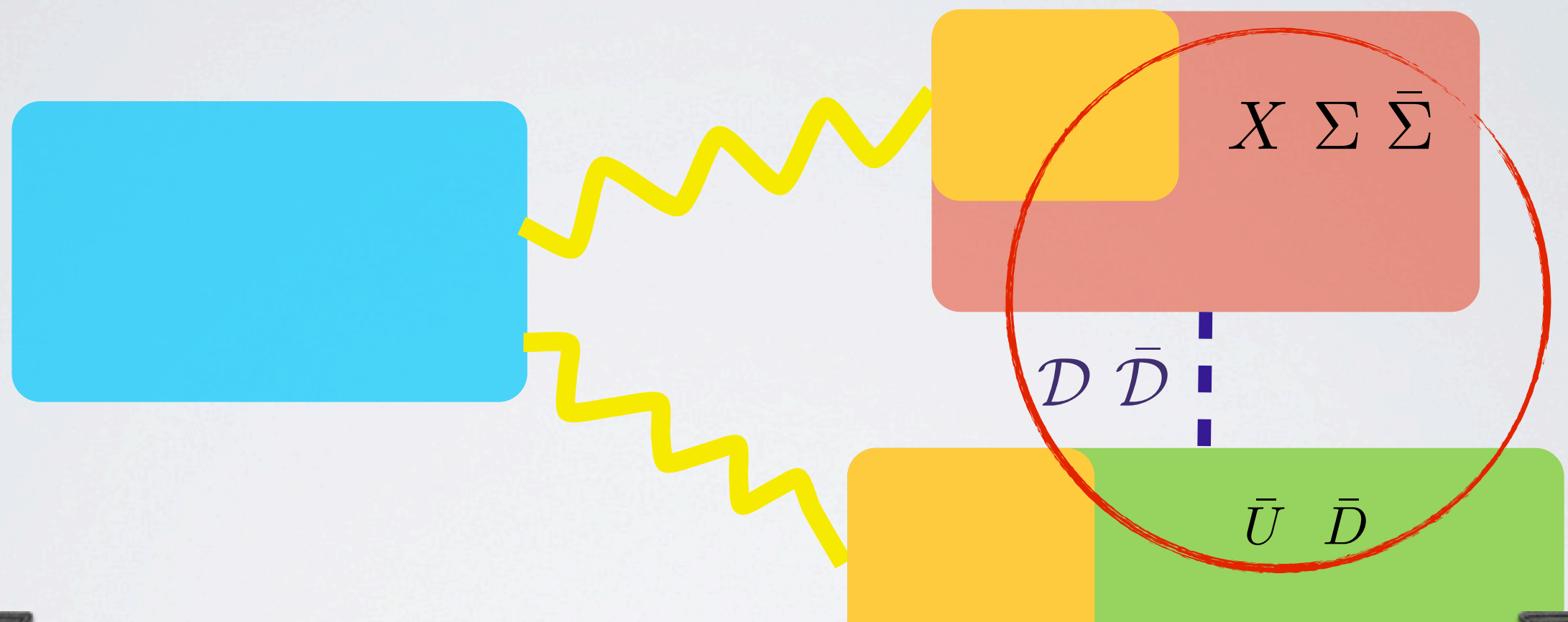
soft RPV





# Breaking & mediation

soft RPV



the potential  $W \supset \bar{U}\bar{D}\bar{\mathcal{D}} + X\mathcal{D}\bar{D} + X\Sigma\bar{\Sigma} + M_{\mathcal{D}}\bar{\mathcal{D}}\mathcal{D}$   
mediates the B-violation (induced by the R-symm breaking) to  
the visible sector

# The UDD A-term

	$SU(3)_c$	$U(1)_Y$	$U(1)_H$	$R$
$\bar{U}$	$\bar{3}$	$-2/3$	0	1
$\bar{D}$	$\bar{3}$	$1/3$	0	1
$\bar{\mathcal{D}}$	$\bar{3}$	$1/3$	0	0
$\mathcal{D}$	3	$-1/3$	0	2
$X$	1	0	0	-1
$\Sigma$	1	0	1	3/2
$\bar{\Sigma}$	1	0	-1	3/2

$$W \supset \bar{U}\bar{D}\bar{\mathcal{D}} + \textcolor{red}{X}\textcolor{blue}{\mathcal{D}}\bar{D} + \textcolor{red}{X}\Sigma\bar{\Sigma} + M_{\mathcal{D}}\bar{\mathcal{D}}\mathcal{D}$$

integrating out the heavy mediator

$$W \supset \frac{\bar{U}\bar{D}\bar{\mathcal{D}}}{M_{\mathcal{D}}} \textcolor{red}{X} + \textcolor{red}{X}\Sigma\bar{\Sigma}$$

$\langle \textcolor{red}{X} \rangle = 0$ , the RPV coupling only comes from the A-term

$$\mathcal{L}_{RPV} = \frac{\tilde{\bar{U}}\tilde{\bar{D}}\tilde{\bar{\mathcal{D}}}}{M_{\mathcal{D}}}(\tilde{\Sigma}\tilde{\Sigma})^*$$



# The UDD A-term

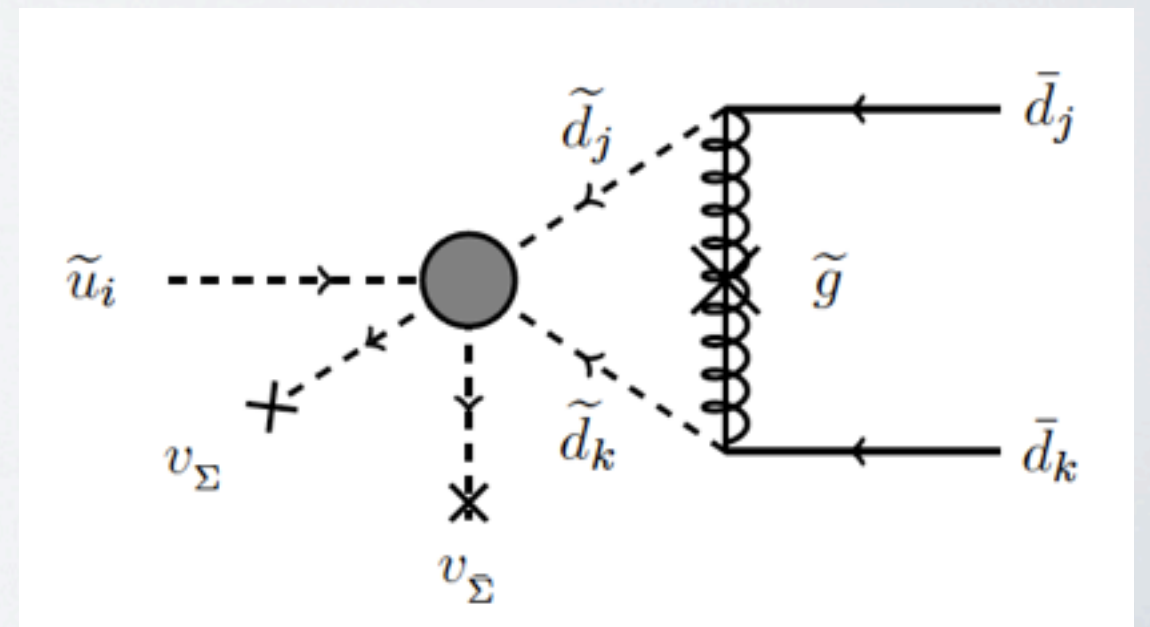
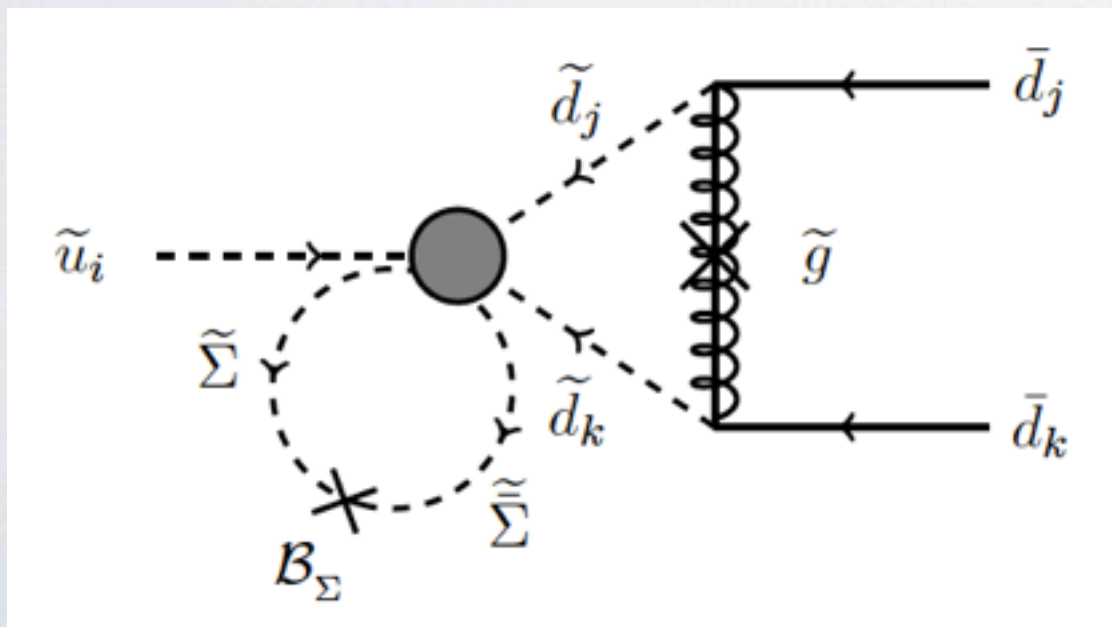
$$\mathcal{L}_{RPV} = \kappa_{i[j} \kappa'_{k]} \epsilon^{abc} \frac{\tilde{U}_a^i \tilde{D}_b^j \tilde{D}_c^k}{M_{\mathcal{D}}} (\tilde{\Sigma} \tilde{\Sigma})^*$$

R-breaking B-term

$$\mathcal{L} \subset \mathcal{B}_{\Sigma} \tilde{\Sigma} \tilde{\Sigma}$$

Radiatively induced VEV

$$\langle \tilde{\Sigma} \tilde{\Sigma} \rangle \simeq m_{soft}^2$$

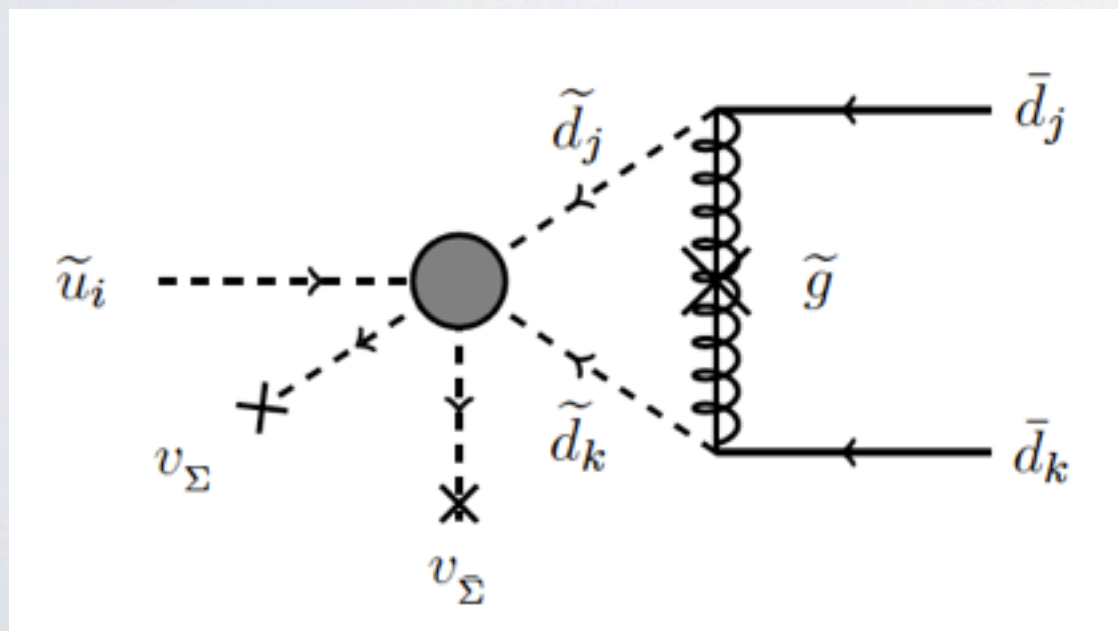


# The $\langle \Sigma \rangle$ model

$$\mathcal{L}_{RPV} = \frac{\tilde{U} \tilde{D} \tilde{D}}{M_{\mathcal{D}}} (\tilde{\Sigma} \tilde{\tilde{\Sigma}})^* + \boxed{V(\tilde{\Sigma}, \tilde{\tilde{\Sigma}})}$$

when  $\Sigma$  gets a tachyonic mass (assume the same mass for simplicity)

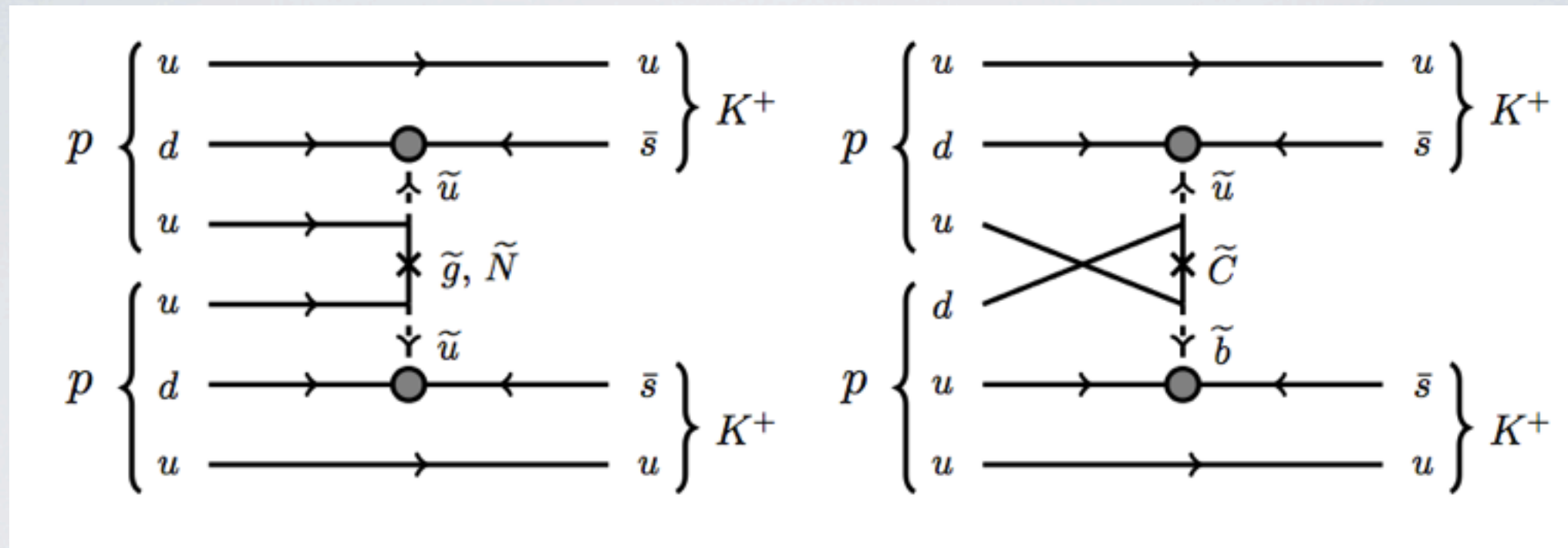
$$V(\tilde{\Sigma}, \tilde{\tilde{\Sigma}}) = -m_{\Sigma}^2 (|\tilde{\Sigma}|^2 + |\tilde{\tilde{\Sigma}}|^2) + \frac{g_H^2}{2} \left( |\tilde{\Sigma}| - |\tilde{\tilde{\Sigma}}|^2 \right)^2 + \eta^2 \left( |\tilde{\Sigma} \tilde{\tilde{\Sigma}}|^2 + |\tilde{X} \tilde{\Sigma}|^2 + |\tilde{X} \tilde{\tilde{\Sigma}}|^2 \right)$$



$$\lambda'' \simeq \frac{\alpha_s}{8\pi} \frac{v_{\Sigma}^2}{M_{\mathcal{D}} M_{\tilde{g}}}$$



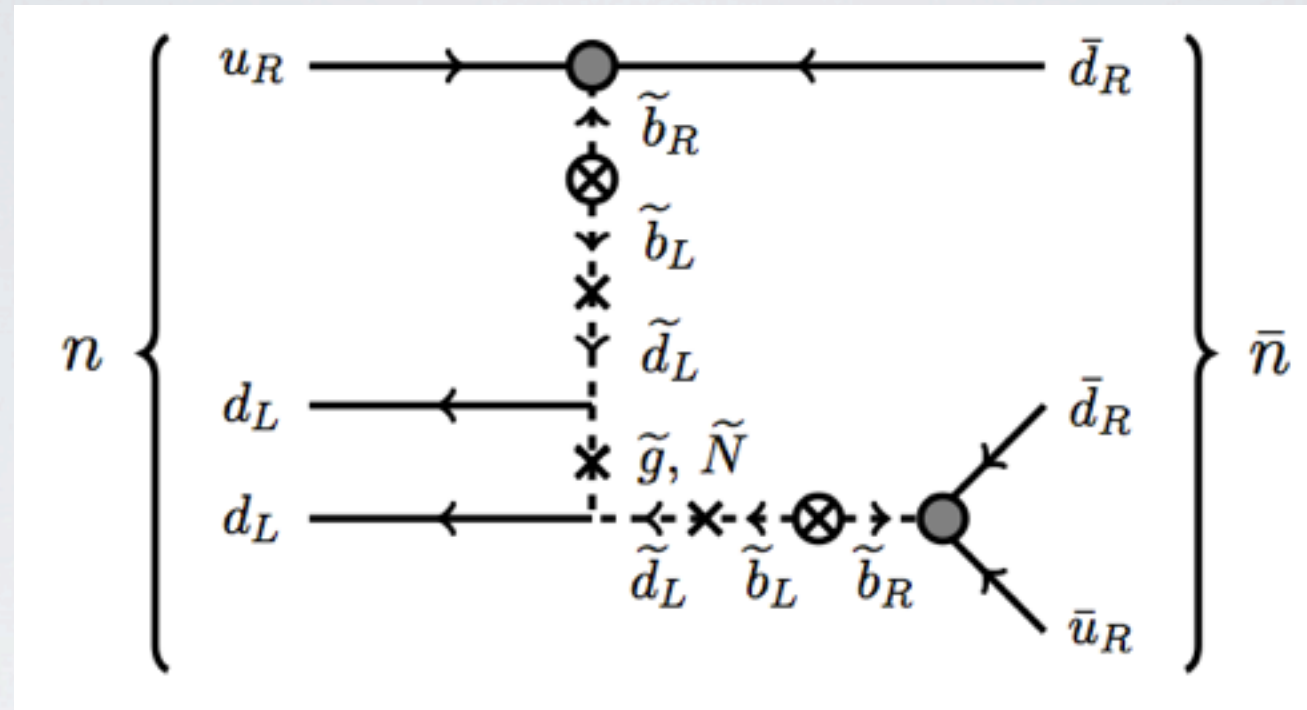
# Di-nucleon decay



$$\Gamma_{pp \rightarrow KK} \sim \rho_N \frac{128 \pi \alpha_s^2 \Lambda^{10}}{m_p^2 m_{\tilde{u}}^8 M_{\tilde{g}}^2} (\lambda''_{uds})^2$$

$$\lambda''_{uds} \lesssim 2.5 \times 10^{-7} \left( \frac{150 \text{ MeV}}{\Lambda} \right)^{5/2} \left( \frac{M_{\tilde{g}}}{800 \text{ GeV}} \right)^{1/2} \left( \frac{m_{\tilde{u}}}{500 \text{ GeV}} \right)^2$$

# Neutron/anti-neutron oscillation

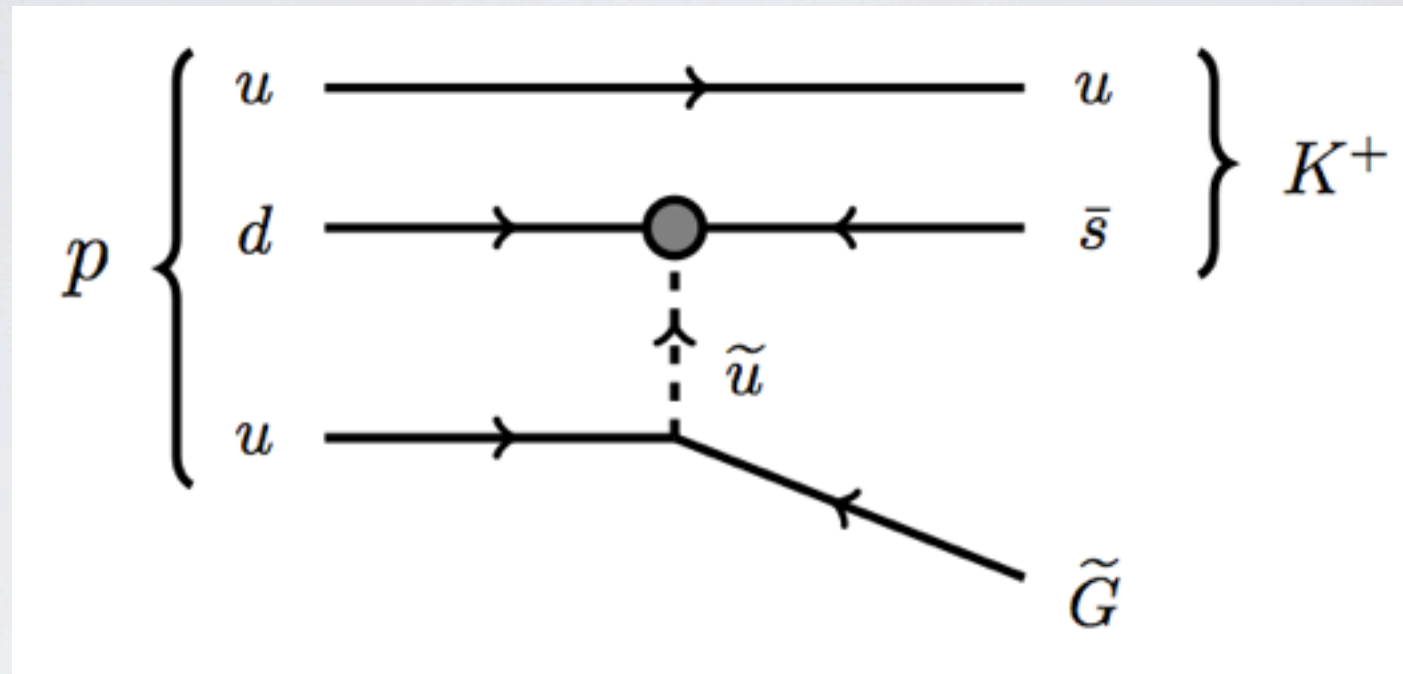


$$\mathcal{M}_{n-\bar{n}} \sim g_s^2 \epsilon^2 \lambda^6 \Lambda \left( \frac{\Lambda}{m_{\tilde{q}}} \right)^4 \left( \frac{\Lambda}{M_{\tilde{g}}} \right) (\lambda''_{udb})^2$$

$$\lambda''_{udb} \lesssim 1.7 \times 10^{-6} \epsilon^{-2} \left( \frac{m_{\tilde{q}}}{500 \text{ GeV}} \right)^4 \left( \frac{250 \text{ MeV}}{\Lambda} \right)^6 \left( \frac{M_{\tilde{g}}}{800 \text{ GeV}} \right)$$



# Proton decay

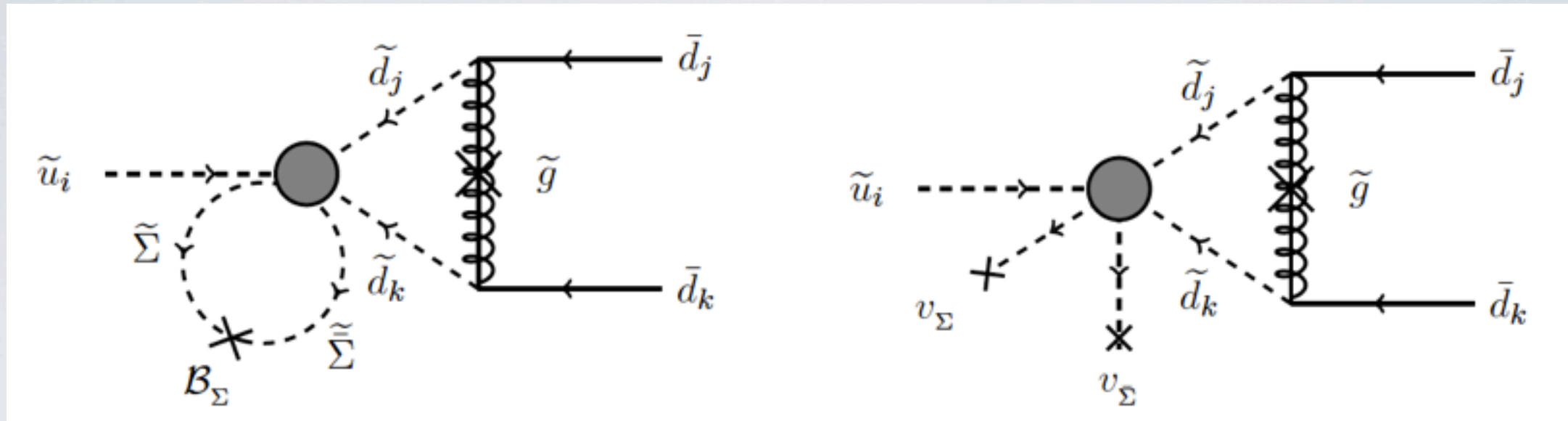


$$\Gamma_{p \rightarrow K^+ \tilde{G}} \sim \frac{m_p}{8\pi} \left( \frac{\Lambda}{m_{\tilde{u}}} \right)^4 \left( \frac{\Lambda^2}{\sqrt{3} m_{3/2} M_{pl}} \right)^2 (\lambda''_{uds})^2$$

$$m_{3/2} \geq 4.7 \text{ MeV} \left( \frac{\Lambda}{250 \text{ MeV}} \right)^4 \left( \frac{500 \text{ GeV}}{m_{\tilde{u}}} \right)^2 \left( \frac{\lambda''_{uds}}{10^{-7}} \right)$$

$$\sqrt{F} \gtrsim 3.2 \times 10^5 \text{ TeV}$$

# The stop decay length



$$\Gamma_{\tilde{t} \rightarrow \bar{q} q} = \frac{m_{\tilde{t}}}{8\pi} \sin^2 \theta_{\tilde{t}} |\lambda''_{tqq}|^2$$

displaced jets are hard to see

$$\lambda''_{tds} > (0.26 - 1.8) \times 10^{-7} \left( \frac{300 \text{ GeV}}{m_{\tilde{t}}} \right)^{1/2}$$

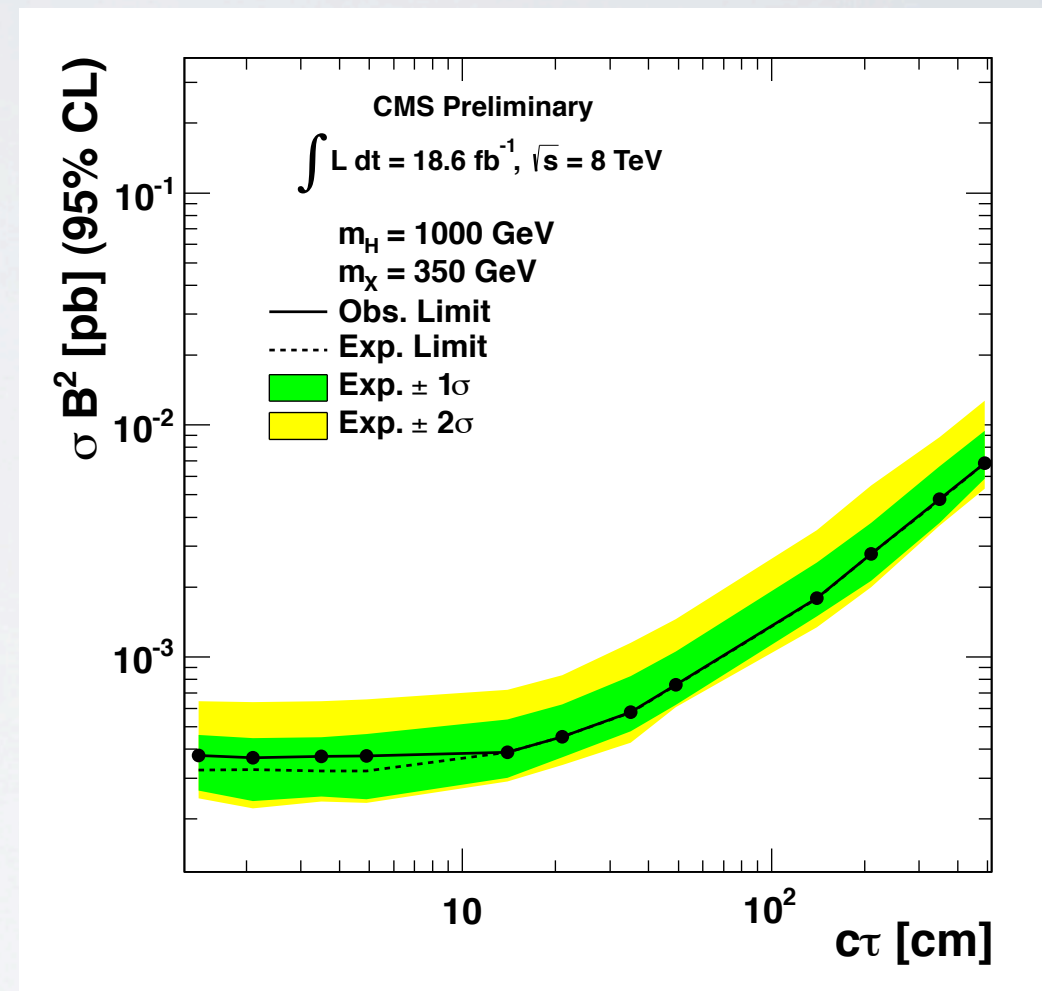
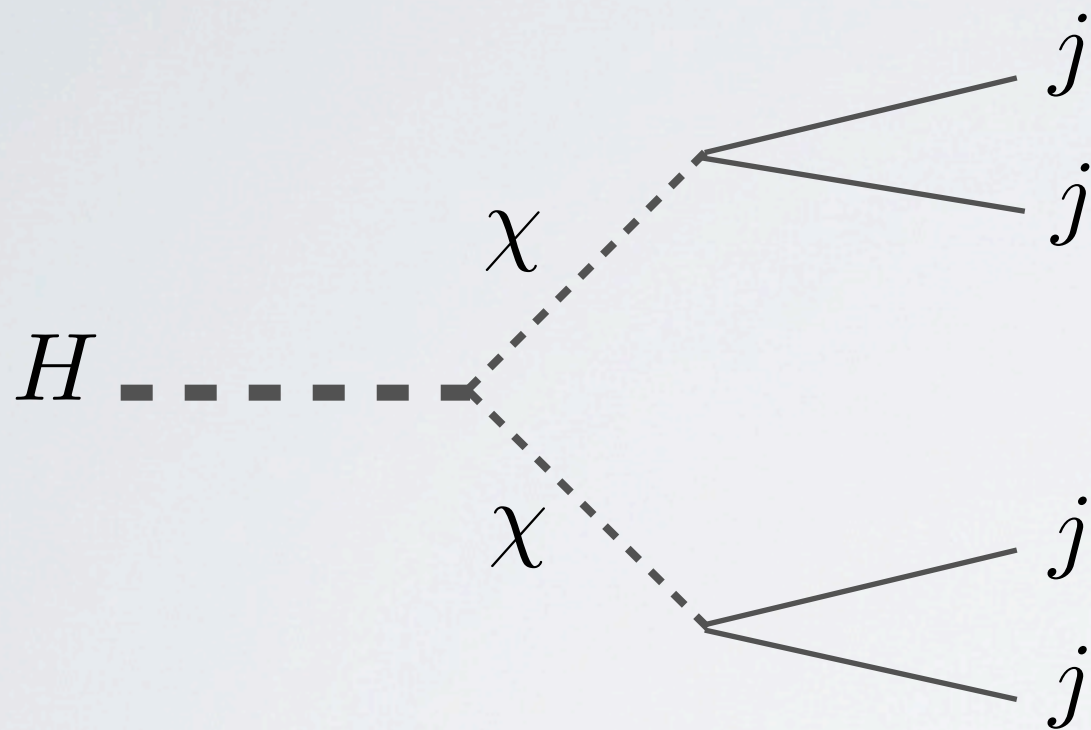
bound for  $\ell_{\tilde{t}} \leq 10 \text{ cm}$

bound for  $\ell_{\tilde{t}} \leq 2 \text{ mm}$



# Constraint on the displaced decay

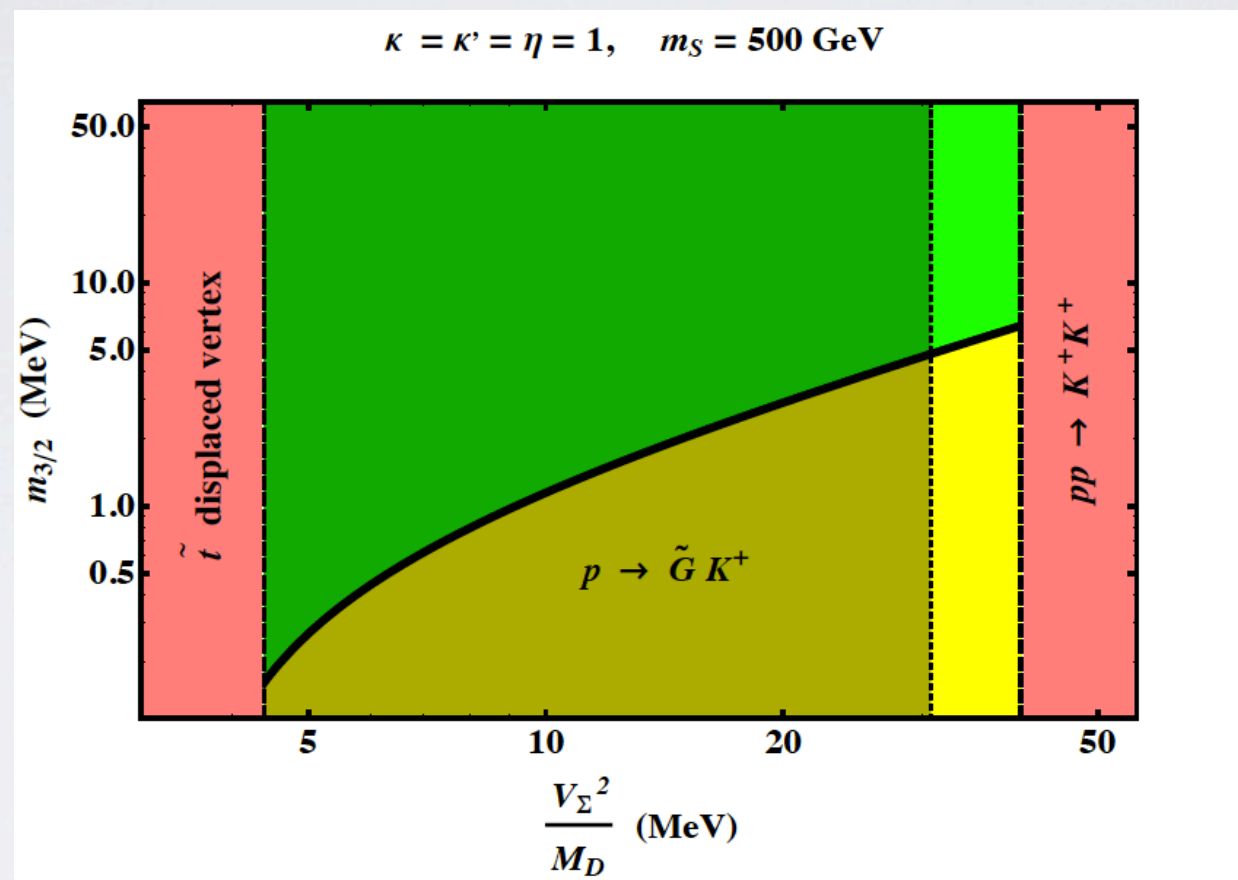
CMS PAS EXO-12-038



the bound is significant now

# Parameter space

For a generic flavor structure



For  $\sqrt{B_\Sigma} \simeq v_\Sigma \simeq TeV$ , the RPV mediator mass

$$M_D \simeq 10^{4-5} \text{ TeV}$$

$$M_D \sim \sqrt{F}$$

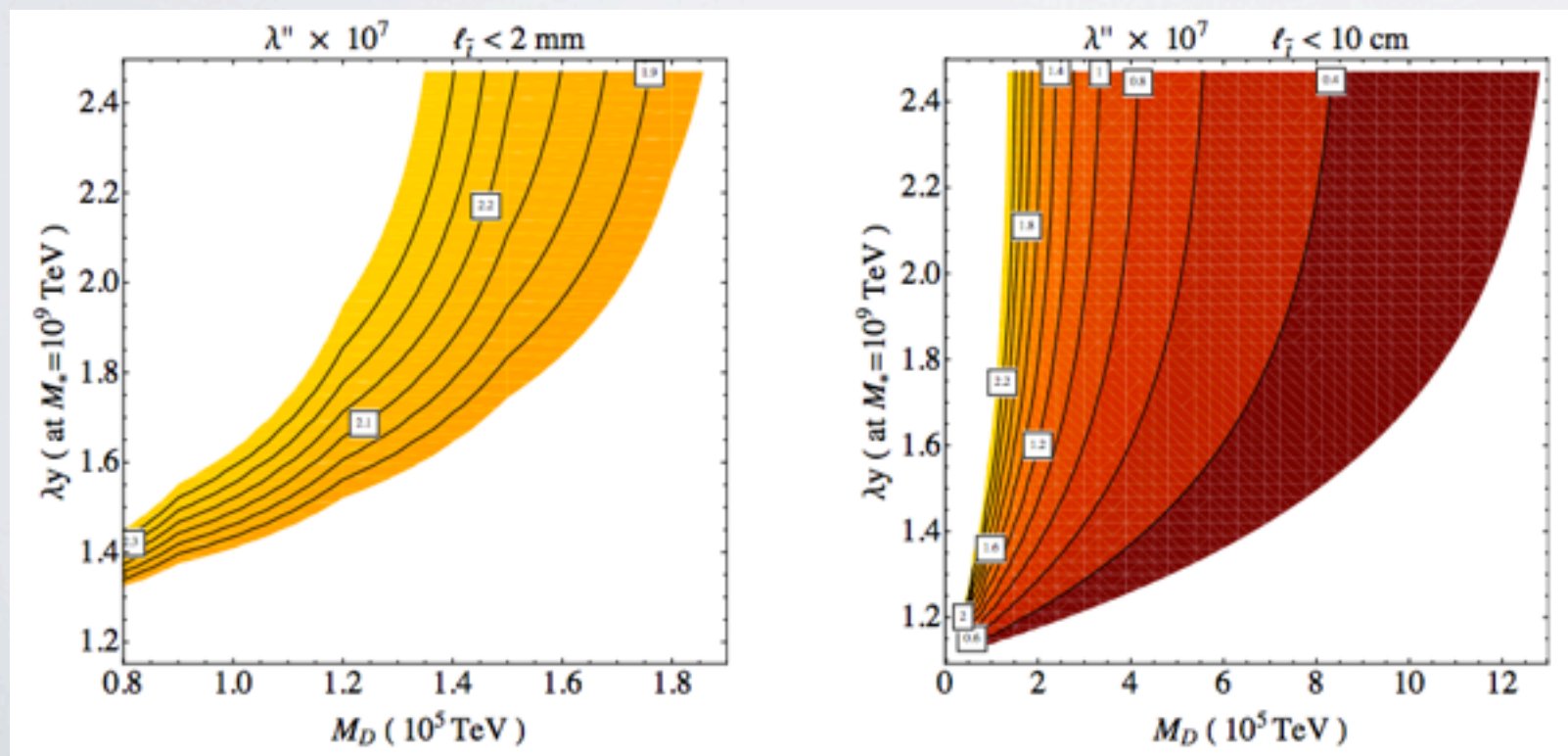


# Mediator mass in the $\langle \tilde{\Sigma} \rangle$ model

to obtain  $\langle \tilde{\Sigma} \rangle$ , we can generate the tachyonic mass  $-m_{\Sigma}^2$  through the RG running with the help of extra matter couplings. for example,

$$W \supset \eta \Sigma X \bar{\Sigma} + \lambda_Y \Sigma Y^2 + \lambda_{\bar{Y}} \bar{\Sigma} \bar{Y}^2$$

The size of  $\langle \tilde{\Sigma} \rangle$  + experimental bounds set the upper/lower bounds on the mediator mass



here we assume

$$\sqrt{F} = 4 \times 10^5 \text{ TeV}$$

from these plot

$$M_D \sim \sqrt{F}$$

is allowed!

# Dark Matter





# Gravitino Dark Matter

In models with baryonic RPV, the LSP can be stable if it's lighter than hadrons

- the  $\mathcal{O}(10)$  MeV scale gravitino can be a thermally produced DM
- no additional non-thermal productions due to the RPV decay

$$\Omega_{3/2} h^2 \simeq 0.1 \left( \frac{T_R}{10^5 \text{ GeV}} \right) \left( \frac{m_{3/2}}{20 \text{ MeV}} \right)^{-1} \left( \frac{M_{\tilde{g}}}{800 \text{ GeV}} \right)^2$$

M.Boltz, A. Brandenburg and W. Buchmuller (2000)

# To conclude...





# To conclude

It's nice to think about the RPV

"softly"

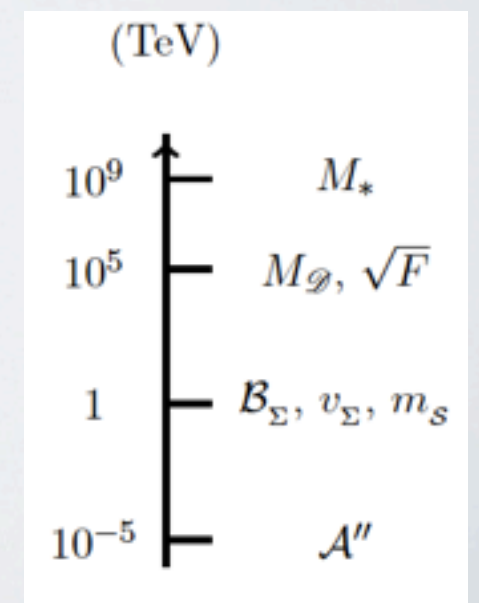
In the example we show here

no additional symmetry required to forbid RPV (use R-symmetry)

no extra mass scales or small couplings put in by hand

gives a dark matter candidate

based on the gauge mediation setup



# BACKUP



# Experimental Constraints

upper bound on  $\lambda''$  (want the process to happen slower)

di-nucleon decay  $\tau_{pp \rightarrow KK} \geq 1.7 \times 10^{32} \text{ yrs}$

neutron/anti-neutron oscillation  $\tau_{n-\bar{n}} \geq 2.44 \times 10^8 \text{ sec}$

lower bound on  $\lambda''$  (want the stop to decay faster)

stop decay length  $\ell_{\tilde{t}} \leq 2 \text{ mm}$  (prompt)  $\ell_{\tilde{t}} \leq 10 \text{ cm}$  (displaced)

lower bound on the ~~SUSY~~ scale (a smaller gravitino coupling)

proton decay into gravitino  $\tau_{p \rightarrow K + \nu} \geq 2.3 \times 10^{33} \text{ yrs}$