



Prompt fission neutron and gamma-ray properties in a Monte-Carlo Hauser-Feshbach framework

Ionel Stetcu

Theoretical Division

Los Alamos National Laboratory

PRC **87** (2013) 014617

PRC **88** (2013) 044603

PRC **90** (2014) 024617

Main collaborators: T. Kawano, P. Talou, M. Jandel

Outline

- Motivation
- The Monte-Carlo Hauser-Feshbach method
- Results for prompt particles, discussion select parameters:
 - ◆ Initial spin distribution
 - ◆ Excitation energy sharing between fragments
 - ◆ Sensitivities to other parameters
- Summary and outlook

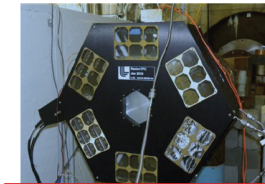
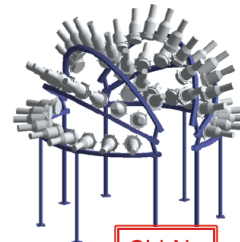
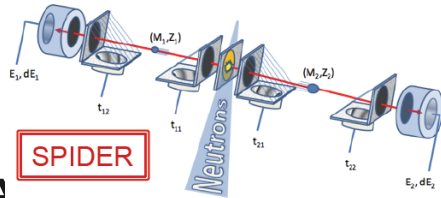
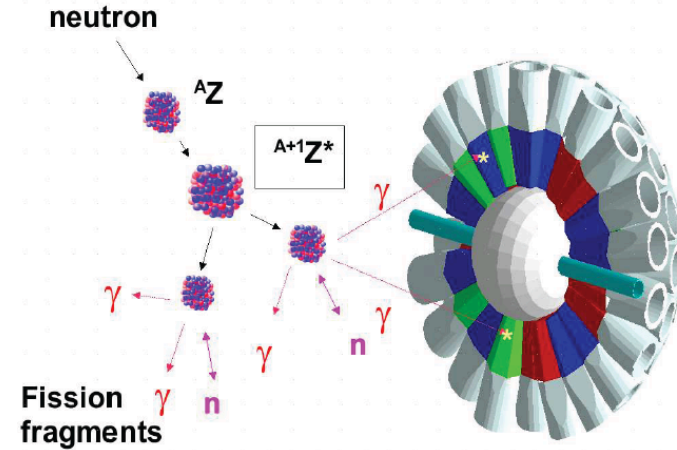
Motivation

- ❖ Basic science:
 - ◆ Understand the pre- and post-scission physics
 - ◆ Interpret experimental data
 - ◆ Provide guidance on detector design

- ❖ Applications:
 - ◆ Nuclear energy: future reactors (new fuel compositions, new geometries, etc.)
 - ◆ Existing fuel cycle (safety, waste management, etc.)
 - ◆ Nuclear forensics
 - ◆ Astrophysics (reaction networks)

Experiment

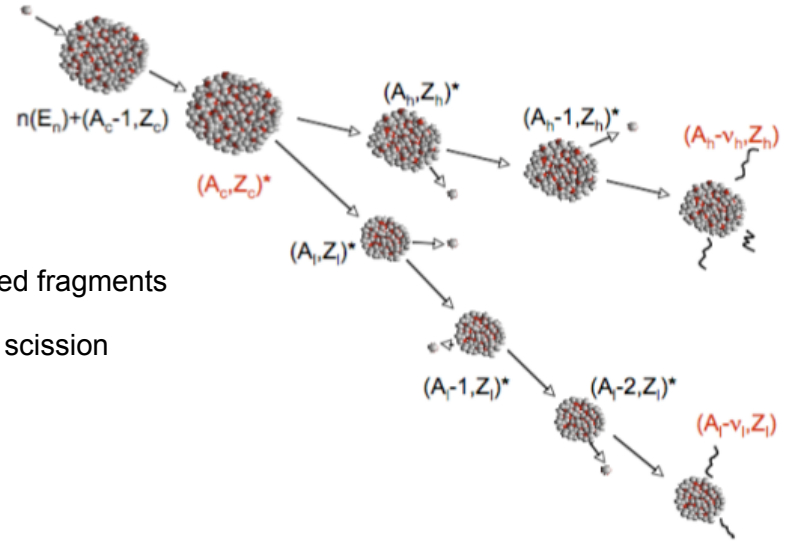
- ◆ Spectroscopy: GAMMASPHERE (binary/ternary fission) – ANL, BNL
- ◆ Calorimetry:
 - ❖ DANCE – n-induced fission
 - ❖ fusion-fission reactions (Dubna)
 - ❖ Crystal ball 162xNaI(Tl) 4π array (Darmstadt)
- ◆ See talks in FIESTA2014: R.C.Haight, N.Colonna, A.Tsinganis, F.Tovesson, M.Jandel, A.Oberstedt, J. Ullmann etc.



Fission simulation

- Assumptions:
 - ◆ Prompt fission products emitted from the fully accelerated fragments
 - ◆ No emission occurs during the evolution from saddle to scission
 - ◆ No emission at the neck rupture
 - ◆ No time information (stop at the ground/isomeric state)
 - ◆ Fission fragments are compound nuclei

- C++ code (MPI implementation) CGMF=CGM+FFD
 - ◆ deterministic and Monte-Carlo modes
 - ◆ similar to DICEBOX at low energies
 - ◆ other similar implementations: FREYA (LLNL), FIFRELIN (CEA), GEF (Schmidt)



Hauser-Feshbach for fission fragments

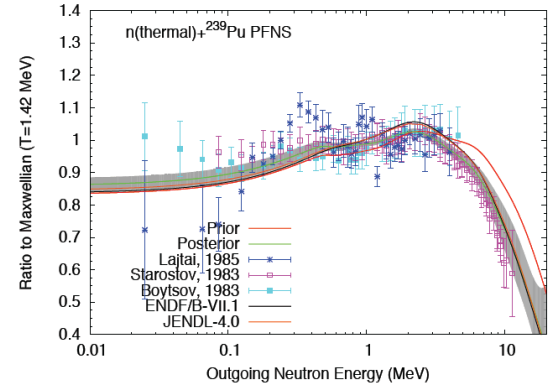
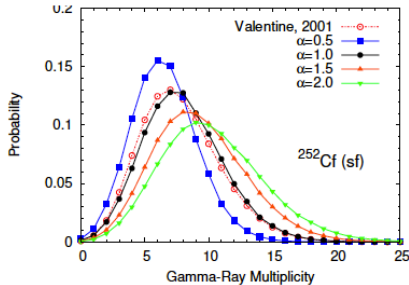
Treat fission fragments as compound nuclei

Description of:

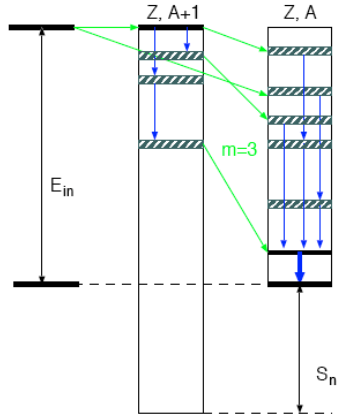
- average prompt fission neutron spectrum
- average prompt fission neutron multiplicity
- $P(\nu)$, $\nu(A)$
- prompt gamma observables
- correlations between particles
- Same approach applicable to describe beta-delayed neutrons/gammas

Complication: more parameters, some not well known

Madland-Nix / Los Alamos model



Hauser-Feshbach formalism for n-induced reactions



- Neutron emission probability:

$$P(\epsilon_n)dE \propto T_n(\epsilon_n)\rho(Z, A - 1, E - \epsilon_n - S_n)$$

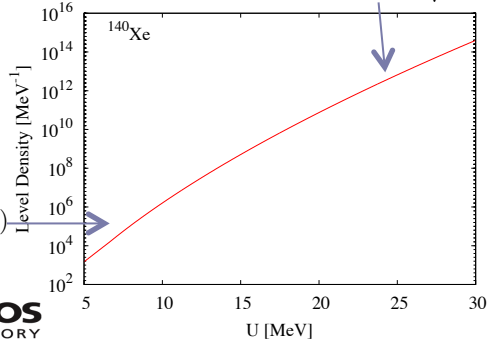
- ✓ Transmission coefficients computed using an optical model
- ✓ Density of states

- Gamma emission probability:

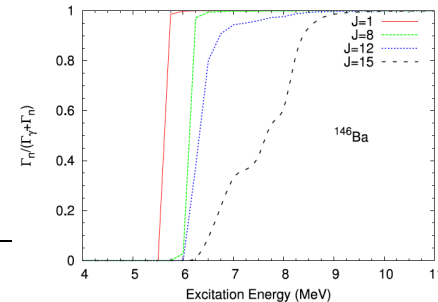
$$P(\epsilon_\gamma)dE \propto T_\gamma(\epsilon_\gamma)\rho(Z, A, E - \epsilon_\gamma)$$

- ✓ Transmission coefficients calculated from the gamma strength function
- ✓ E1, M1 and E2 transitions only
- ✓ Density of states
- ✓ Discrete levels

$$\rho(U) = \frac{1}{12\sqrt{2}\sigma} \frac{\exp(a\sqrt{aU})}{a^{1/4}U^{5/4}}$$



$$\rho(U) = \frac{1}{T} \exp(U/T)$$



Input into the fission simulations

- Experimental Information:

- ◆ Primary fission fragment yields
- ◆ Internal excitation energy

$$\begin{aligned}
 TXE &= Q_f(A_l, Z_l; A_h, Z_h; A_c, Z_c) - TKE \\
 &= M_l + M_h - M_c + E_{inc} + B_n(A_c, Z_c) - TKE
 \end{aligned}$$

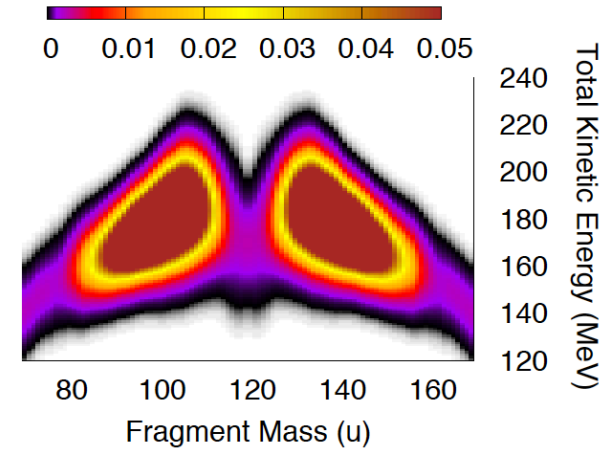
- ◆ Ingredients used in HF calculations (gamma strength functions, discrete levels)

- Theory/Model:

- Charge distribution: from Wahl systematics $Z_p = A_h \frac{Z_c}{A_c} + \Delta Z$
- Parity distribution: assumed equiprobable
- Excitation energy sharing: $R_T = \frac{T_l}{T_h}$
- Initial spin distribution:

$$P(J) \propto (2J + 1) \exp(-J(J + 1)/(2B^2))$$

- Ingredients used in HF calculations (optical model parameters)



NO DIRECT MEASUREMENTS

- de-excitation feeding patterns of the ground-state bands
- angular anisotropy of prompt fission gamma rays
- isomeric ratios

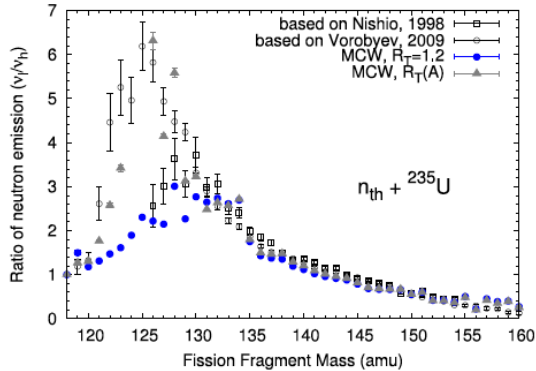
Energy sharing

$$R_T = \frac{T_l}{T_h}$$

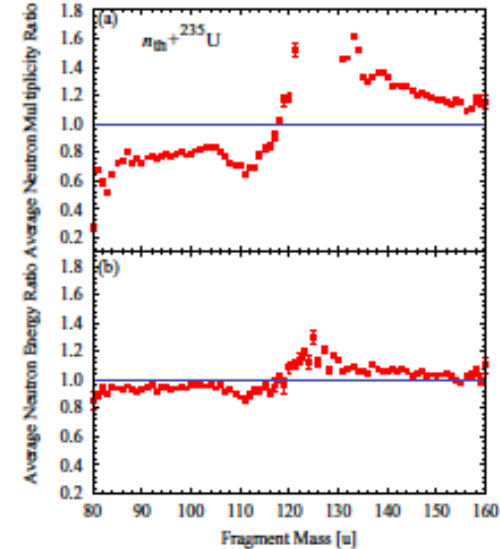
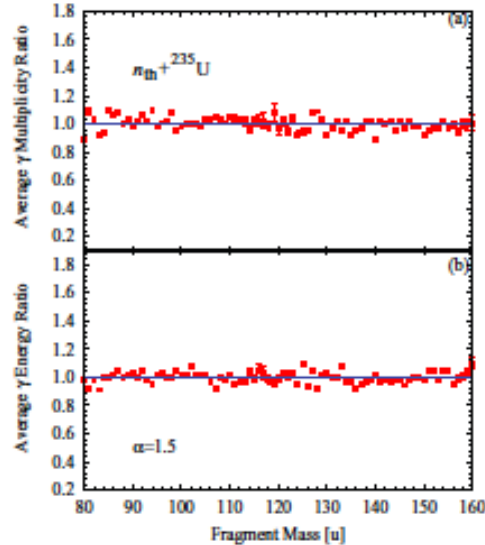
$R_T=1$: thermal equilibrium (like in the Los Alamos model)

$R_T=\text{constant}$

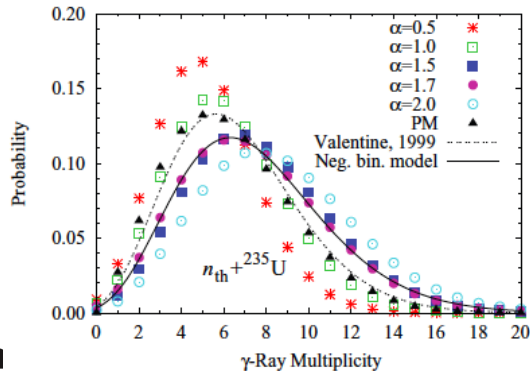
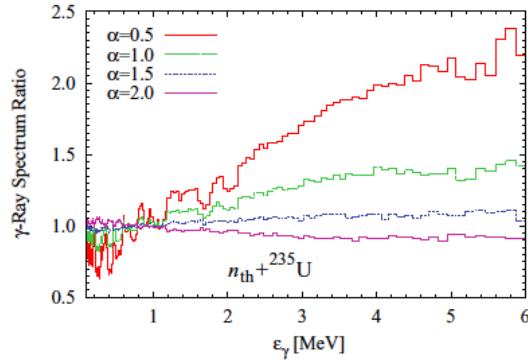
$R_T(A)$



- ❖ symmetric fission: $R_T=1$
- ❖ ~ 130 : maximum (closed shell)
- ❖ >130 R_T decreases to below one (deformation)



Sensitivity to the initial angular momentum

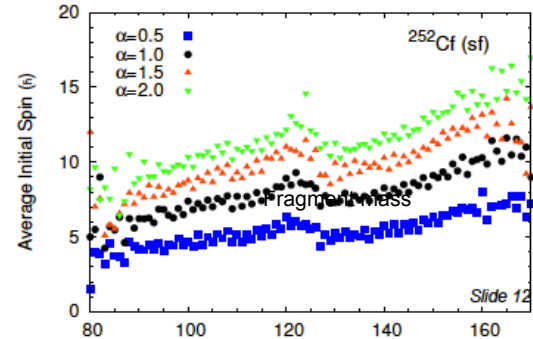


$$P(J) \propto (2J + 1) \exp(-J(J + 1)/(2B^2))$$

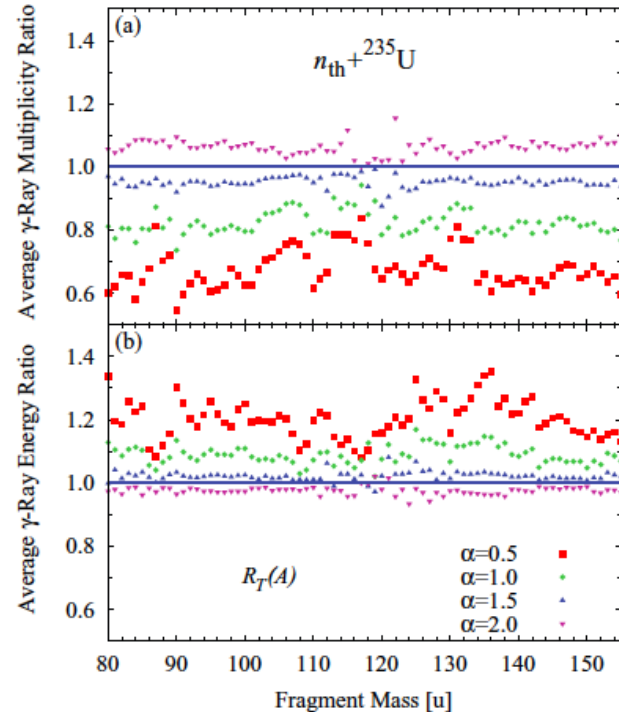
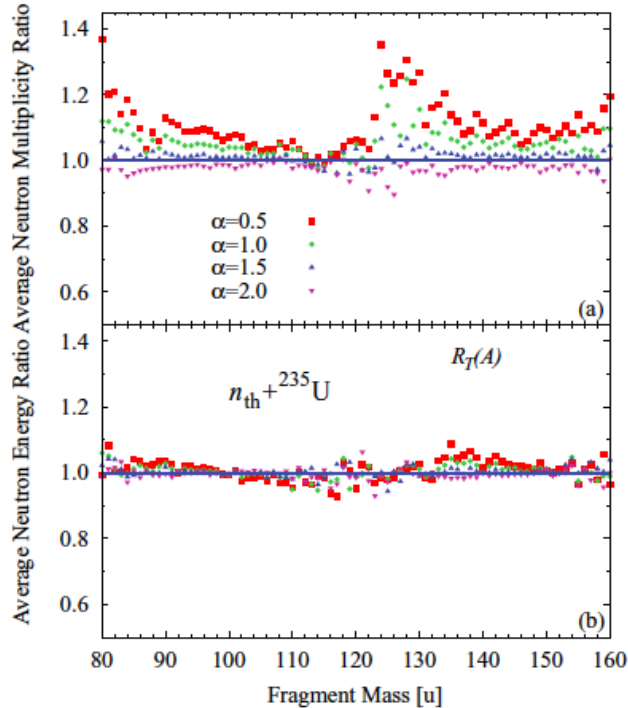
$$B^2 = \frac{IT}{\hbar^2}$$

$$\mathcal{I} = \alpha \mathcal{I}_{rig}^0(Z, A, \beta)$$

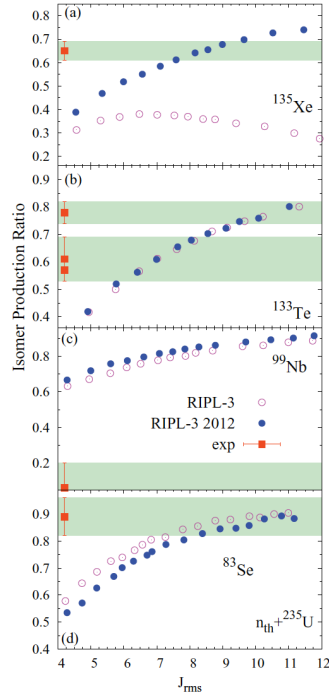
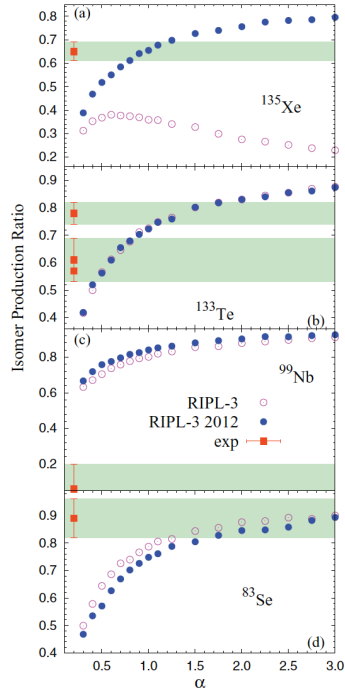
Experimental evidence*: $J_{rms}=5-8$ for LF and 7-10 for HF



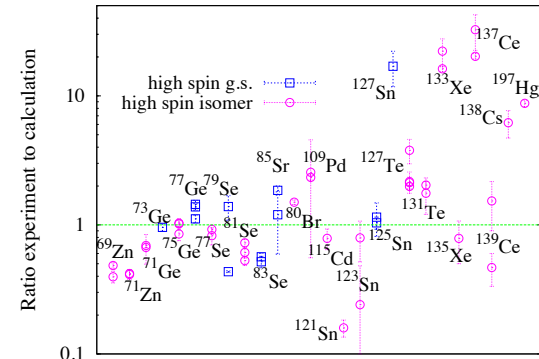
Sensitivity to the initial angular momentum (cont)



Isomeric ratios and the angular momentum

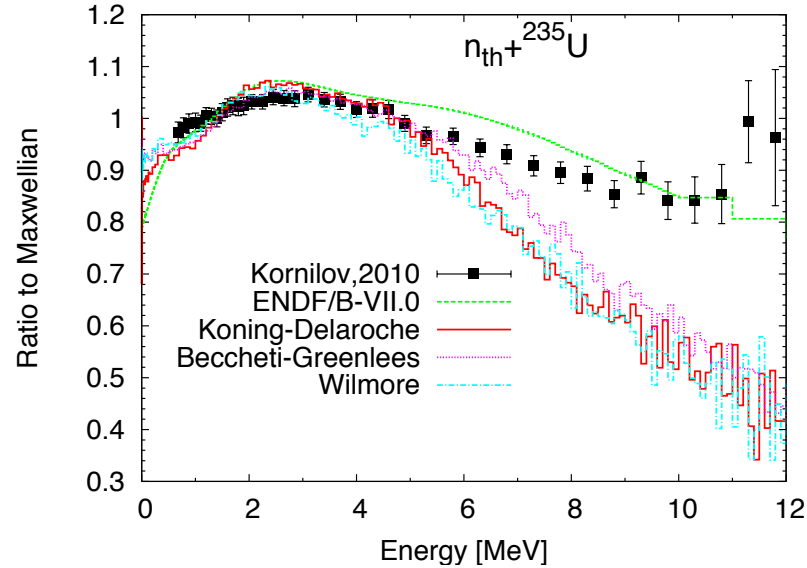


thermal neutron capture on stable nuclei: better handle on initial spin and excitation energy

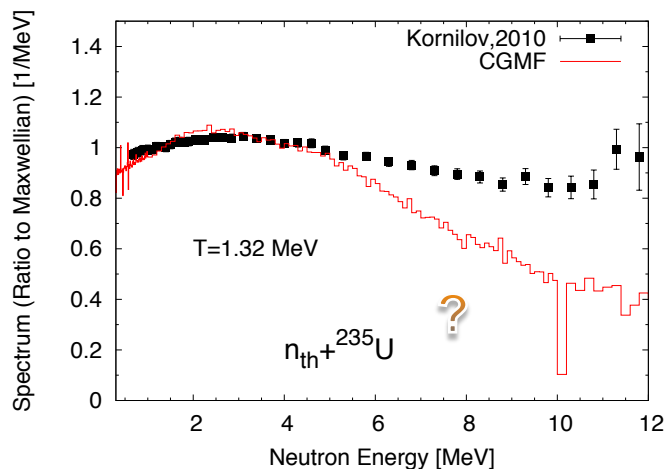
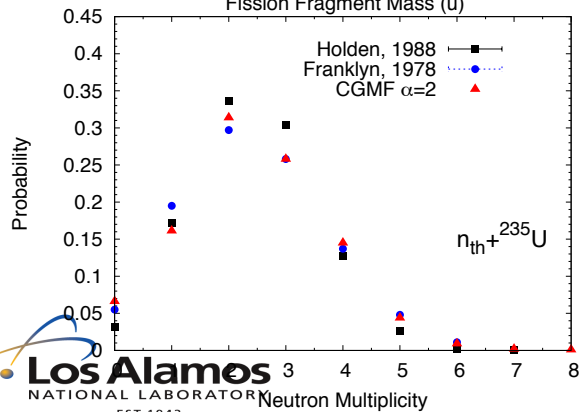
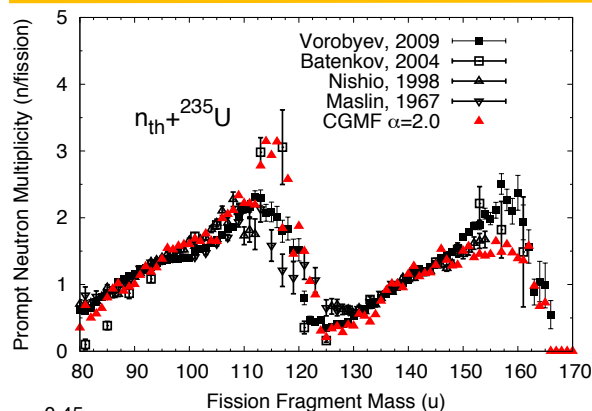


PRC 88 (2013) 044603

Sensitivity to the optical potential



Selected results for $n+^{235}\text{U}$ – neutron observables



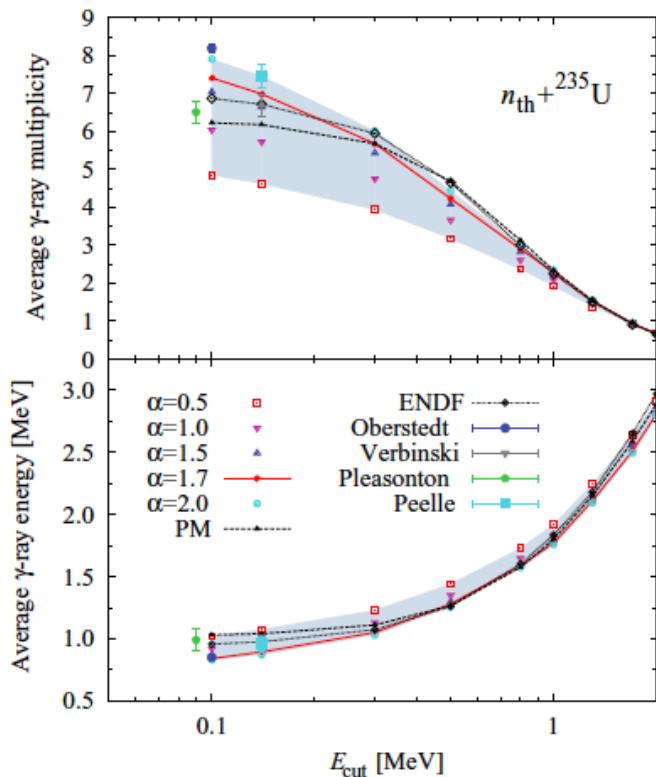
α	ν
1.0	2.598
1.2	2.557
1.3	2.539
1.4	2.524
1.5	2.507
1.7	1.462
2.0	2.435
3.0	2.326
4.0	2.254

Becker et. al., Phys Rev C **87** (2013) 014617

UNCLASSIFIED

Slide 14

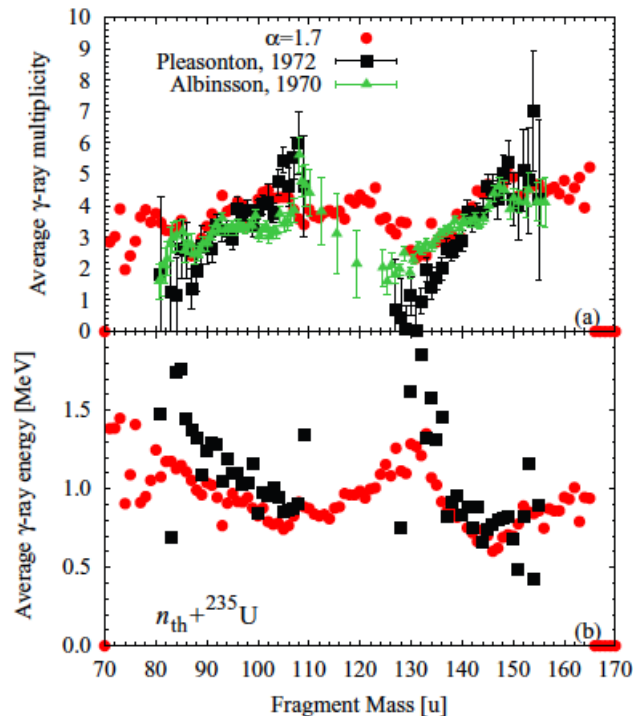
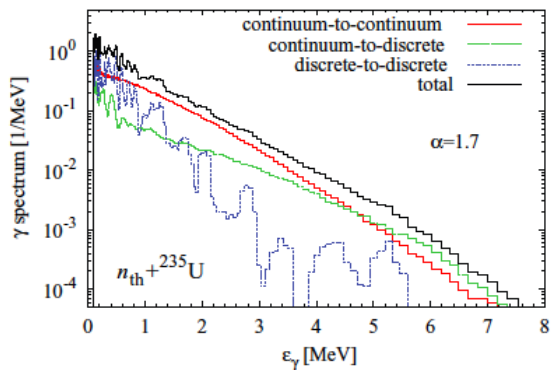
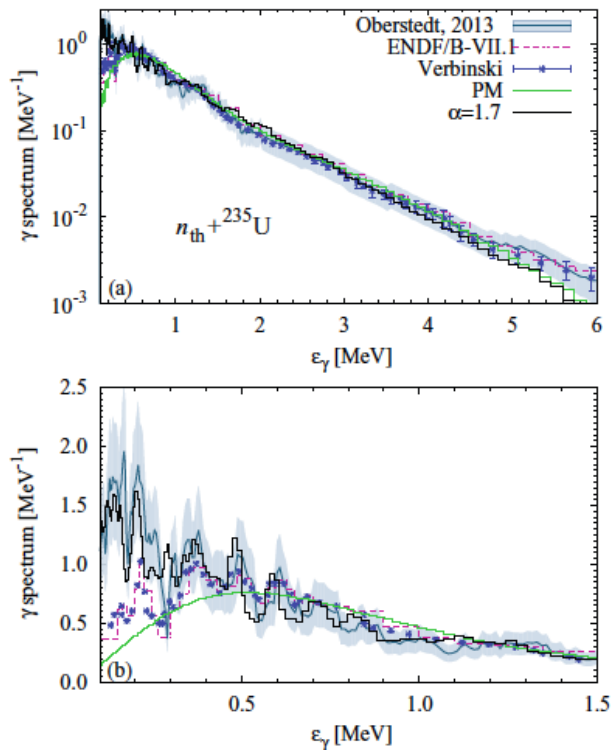
Cutoff γ energy



E_{cut} (MeV)	α					PM	Experiment
	0.5	1.0	1.5	1.7	2.0		
${}^{235}\text{U}(n_{th}, f)$							
0.1	4.85	6.04	7.04	7.41	7.91	6.23	8.19 ± 0.11 [14] 6.51 ± 0.31 [11] ^a
0.14	4.62	5.73	6.65	6.99	7.46	6.18	7.45 ± 0.32 [10] 6.69 ± 0.30 [12] 7.78 ^b
0.3	3.94	4.76	5.43	5.68	6.02	5.68	6.11 ^b
1.0	1.93	2.10	2.24	2.29	2.35	2.34	2.33 ^b
2.0	0.69	0.67	0.66	0.66	0.66	0.67	0.69 ^b
${}^{239}\text{Pu}(n_{th}, f)$							
0.1	5.57	6.95	7.48	7.87	8.39	7.08	7.38 ^c
0.14	5.25	6.52	7.05	7.39	7.88	7.01	7.23 ± 0.30 [12]
0.3	4.40	5.34	5.72	6.38	6.33	6.44	5.95 ^c
1.0	2.15	2.36	2.39	2.56	2.51	2.79	2.17 ^c
2.0	0.76	0.75	0.74	0.74	0.74	1.06	0.72 ^c
${}^{252}\text{Cf}(sf)$							
0.1	5.52	6.74	8.04	8.15	8.68	8.02	8.30 ± 0.08 [13]
0.14	5.23	6.34	7.51	7.64	8.12	7.89	7.8 ± 0.3 [12] 8.01 ^d
0.3	4.23	5.02	5.86	5.95	6.29	6.83	6.45 ^d
1.0	1.99	2.14	2.31	2.33	2.40	2.22	1.90 ^d
2.0	0.73	0.73	0.74	0.74	0.74	0.77	0.67 ^d

UNCLASSIF

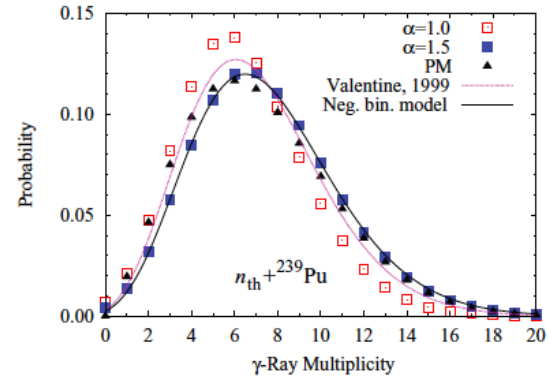
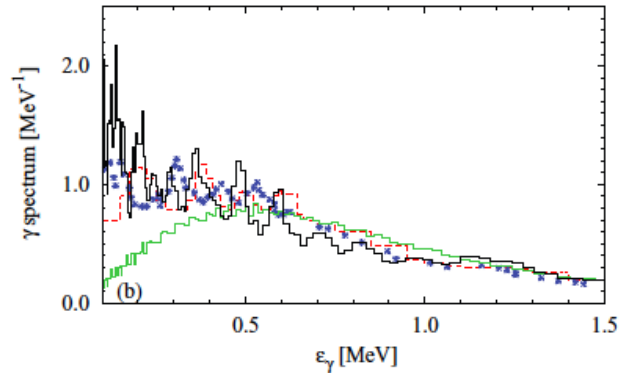
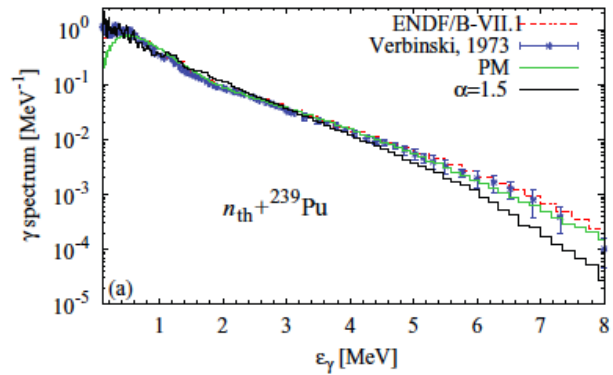
$n_{th} + ^{235}\text{U}$: gamma observables



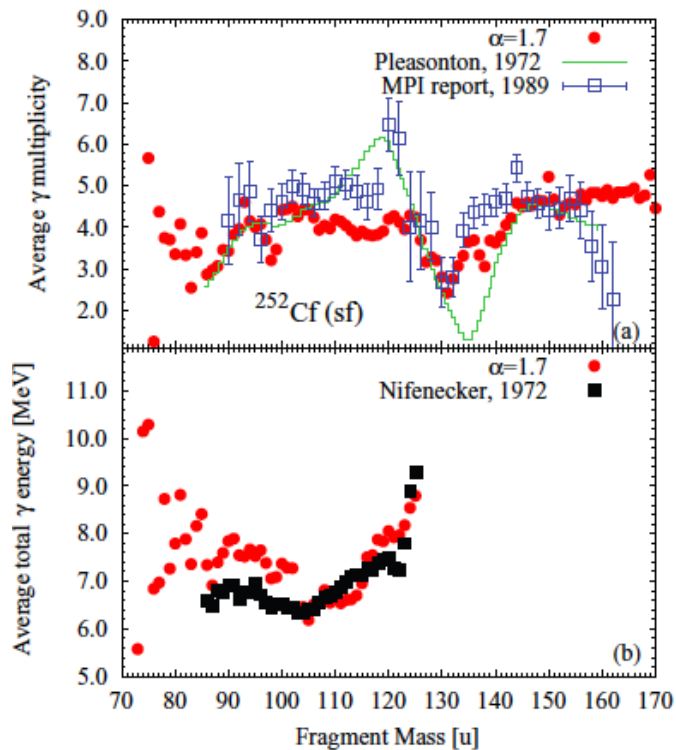
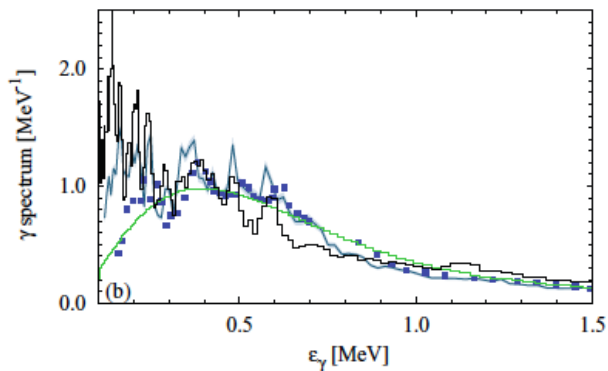
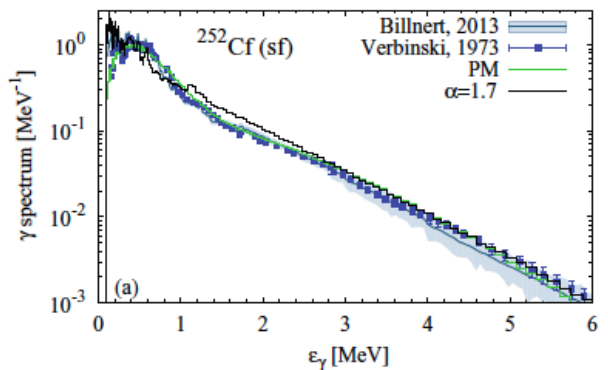
Data from M. Jandel et. al.

UNCLASSIFIED

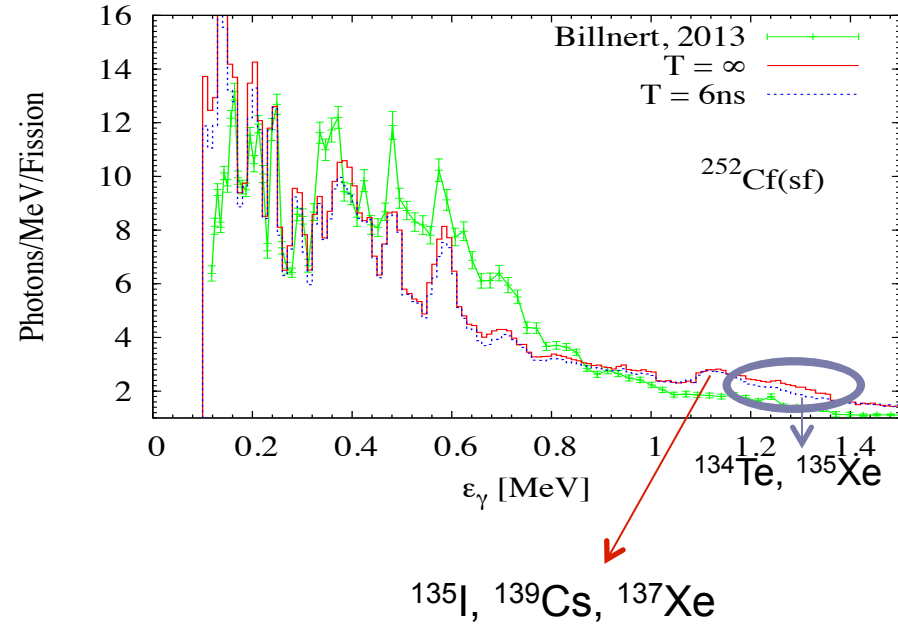
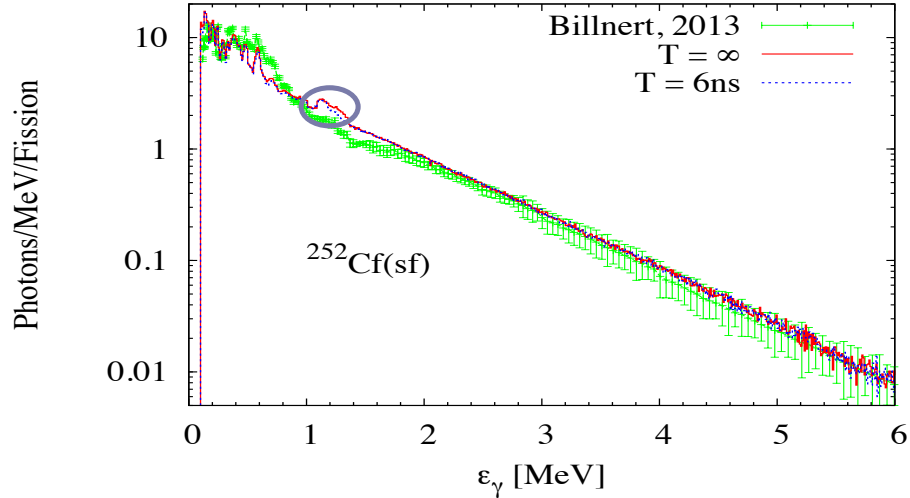
$n_{th} + {}^{239}\text{Pu}$



^{252}Cf (sf)



Isomeric states in CGMF



Summary and outlook

- ◇ De-excitation of fission fragments described within the MCHF formalism
 - Gamma-ray strength
 - OMP for neutron emission
 - Neutron-gamma competition
- ◇ MC histories recorded and used to produce average quantities and for post processing
- ◇ Good quantitative agreement with experimental data
 - ◆ Some discrepancies still exist (neutron/gamma spectra too soft)
- ◇ Requires some fine tuning (many parameters)
- ◇ Future work: extension other actinides and extend the range of incident energies

