



Characteristics of prompt fission γ-ray emission – advances in measurements, evaluations and predictions

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- Historical background the 1970s
- Evaluation of PFGS characteristics
- Renaissance the 2010s
- New evaluation systematics
- Fast neutron induced fission
- Predictions for ²³⁸U(n, f)
- Recent results
- Predictions for ²³⁵U(n, f)
- Conclusions
- Outlook





Historical background Experiments

- First comprehensive studies of prompt fission γ -ray spectra (PFGS) in the 1970s on:
 - n_{th} + ²³³U
 - n_{th} + ²³⁵U
 - n_{th} + ²³⁹Pu
 - ²⁵²Cf (sf)
- Measured PFGS characteristics:
 - $E_{\gamma,tot}$ = average total γ -energy/fission
 - ϵ_{γ} = average γ -energy/photon
 - \overline{v}_{γ} = average γ -multiplicity





Historical background Evaluations

1972: Nifenecker et al. (NPA 189 (1972) 285)

• $E_{\gamma,tot}(\overline{v}_n) = 0.75 \overline{v}_n + 2.0$

2001: Valentine (ANE 28 (2001) 191)

- $E_{\gamma,tot}(\overline{v}_n, A, Z) = \phi(A, Z) \overline{v}_n + 4.0 \text{ (MeV)}$ with $\phi(A, Z) = 2.51(\pm 0.01) - 1.13 \cdot 10^{-5}(\pm 7.2 \cdot 10^{-8}) Z^2 A^{1/2}$
- $\epsilon_{\gamma}(A,Z) = -1.33(\pm 0.05) 119.6 \cdot 10^{-5}(\pm 2.5) Z^{1/3} / A$
- $\overline{v_{\gamma}}(\overline{v_{n}},A,Z) = E_{\gamma,tot}(\overline{v_{n}},A,Z) / \varepsilon_{\gamma}(A,Z)$

Note: A and Z dependences are purely empirical!







- In the 2010s: new PFGS measurements and calculations motivated by NEA high priority request lists for
 - n_{th} + ²³⁵U and n_{th} + ²³⁹Pu
- Investigated processes:
 - ${}^{235}U(n_{th}, f), {}^{239,241}Pu(n_{th}, f), {}^{252}Cf(sf)$
- Experimental groups:
 - LANL DANCE
 - IRMM/Chalmers/KFKI + others
- Theoretical groups (Monte Carlo Hauser Feshbach):
 - CEA Cadarache (Serot, Litaize, Regnier)
 - LANL (Talou et al.)
 - K.-H. Schmidt and others





New results - overview Our work

- Experiments at IRMM and KFKI Budapest:
 - ²⁵²Cf(sf)
 - ²³⁵U(n_{th}, f)
 - ²⁴¹Pu(n_{th}, f)

- R. Billnert et al., PRC 87 (2013)
- A. Oberstedt et al., PRC 87 (2013)
- S. Oberstedt et al., PRC 90 (2014)

- Measured:
 - prompt fission γ-ray spectrum (PFGS)
- Determined:
 - average multiplicity
 - mean energy per photon
 - total photon energy
- Deduced:
 - multiplicity distribution





Experimental setup:

fission trigger: photons:





PPAC BaF₂ array



Experimental setup:

fission trigger: photons:

PFGS:



measured













0.5

 E_{γ} (MeV)

fission trigger: photons:

10⁻²

10⁻³

0.1

PFGS:

setup:

5



Experimental setup:

fission trigger: photons:

PFGS:

multiplicity distribution:





252Cf(SF) Chyzh et al. Chyzh

0.12

0.1

0.08

0.06

0.04

0.02

measured

 $\overline{\mathbf{v}}_{\mathbf{v}}$







Experimental setup:

fission trigger: photons:

PFGS:

multiplicity distribution:





measured

Photons / (MeV fission)

10

10

10

10

10⁻³







General impression for the fissioning systems $^{252}Cf(sf)$, $^{235}U(n_{th}, f)$ and $^{241}Pu(n_{th}, f)$

• $E_{\gamma,tot}$ and ϵ_{γ} :

good agreement between our results and those from the early 1970s, while values from DANCE are higher

• $\overline{\mathbf{v}_{\gamma}}$: our results agree well with the 1970s results, but the DANCE values are somewhat lower

 Impact of our new results on evaluation according to Valentine?





Observe: \overline{v}_n taken from experiments





Observe: \overline{v}_n taken from experiments and ENDF/B-VII.1





Observe: \overline{v}_n taken from experiments. and ENDF/B-VII.1





Observe: \overline{v}_n taken from experiments. and ENDF/B-VII.1



























Observe: \overline{v}_n taken from experiments







Observe: \overline{v}_n taken from experiments and ENDF/B-VII.1

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Observe: \overline{v}_n taken from experiments. and ENDF/B-VII.1

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Observe: \overline{v}_n taken from experiments. and ENDF/B-VII.1

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- PFGS characteristics as function of A and Z of the compound system
- Agreement between new experimental results and "Valentine's evaluation" is rather good
- Parameters might need an adjustment
- Estimate (interpolations/extrapolation) of PFGS characteristics is possible for nuclei, which are not accessible experimentally
- However: only valid for thermal neutron induced and spontaneous fission?
- Attempt: fast neutron induced fission!
- Example below: ²³⁸U(n, f)!





Fast neutron induced fission Motivation

Why n + 238 U PFGS?

- Important nuclide for fast reactors
- one of six isotopes in the focus of the CIELO pilot project
- First preliminary experimental results from CEA in Bruyères-le-Châtel are available
 - at $E_n = 1.7$ and 15.6 MeV (BGO)
 - as well as E_n = 1.7 and 5.2 MeV (BGO), new! (Laborie et al., private communication)
- New experiment performed recently at IPN Orsay
 - LICORNE facility, covering energy range between $E_n = 0.7$ and 4 MeV
 - First preliminary results obtained







²³⁸U(n, f) PFGS characteristics



Prompt fission neutron multiplicity



- prompt fission neutrons from ENDF/B-VII.1
- pre-fission neutrons subtracted
- prompt neutrons from fragments for PFGS characteristics only those may be related to prompt fission γ-ray emission!





• from PFGS systematics as function of A and Z

$$\begin{array}{c} (E_{\gamma,tot} - 4)/\overline{v}_n \\ \epsilon_{\gamma} \\ \overline{v}_{\gamma} / \overline{v}_n \end{array} \right\} for n + {}^{238}U$$





from PFGS systematics as function of A and Z







• from PFGS systematics as function of A and Z

$$\begin{array}{c} (E_{\gamma,tot} - 4)/\overline{v}_n \\ \epsilon_{\gamma} \\ \overline{v}_{\gamma} / \overline{v}_n \end{array} \right\} for n + 238U$$

• using $\overline{v}_n(E_n) = \overline{v}_{ff}(E_n)$





• from PFGS systematics as function of A and Z

$$\begin{array}{c} (E_{\gamma,tot} - 4)/\overline{v}_n \\ \epsilon_{\gamma} \\ \overline{v}_{\gamma} / \overline{v}_n \end{array} \right\} for n + {}^{238}U$$

• using
$$\overline{v}_n(E_n) = \overline{v}_{ff}(E_n)$$

• assuming: only energy dependence = $\overline{v}_{ff}(E_n)$





- from PFGS systematics as function of A and Z

$$\begin{array}{c} (E_{\gamma,tot} - 4)/\overline{v}_n \\ \epsilon_{\gamma} \\ \overline{v}_{\gamma} / \overline{v}_n \end{array} \right\} for n + 238 U$$

• using
$$\overline{v}_n(E_n) = \overline{v}_{ff}(E_n)$$

- assuming: only energy dependence = $\overline{v}_{ff}(E_n)$
- calculating $E_{\gamma,tot}(E_n)$ $\overline{v}_{\gamma}(E_n)$ $\epsilon_{\gamma}(E_n) = E_{\gamma,tot}(E_n)/\overline{v}_{\gamma}(E_n)$




²³⁸U(n, f) PFGS characteristics Calculating energy dependence

• from PFGS systematics as function of A and Z

$$\begin{array}{c} (E_{\gamma,tot} - 4)/\overline{v}_n \\ \epsilon_{\gamma} \\ \overline{v}_{\gamma} / \overline{v}_n \end{array} \right\} for n + 238 U$$

• using
$$\overline{v}_n(E_n) = \overline{v}_{ff}(E_n)$$

- assuming: only energy dependence = $\overline{v}_{ff}(E_n)$
- calculating $E_{\gamma,tot}(E_n)$

$$v_{\gamma}(E_n)$$

 $\varepsilon_{\gamma}(E_n) = E_{\gamma,tot}(E_n)/\overline{v}_{\gamma}(E_n)$

- comparison with model calculations
- comparison with preliminary experimental results







- Tudora: Point-by-Point model
- Litaize et al.: FIFRELIN code (ND 2013, to appear in NDS)
- Laborie et al.: preliminary results (2014)







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Mean energy per photon



- Litaize et al.: FIFRELIN code (calculated by $E_{\gamma,tot}/\overline{v_{\gamma}}$)
- Laborie et al.: preliminary results (2014)



Next summary ...



- Predictions of PFGS characteristics as function of incident neutron energy have been presented for ²³⁸U(n, f)!
- Investigated energy range: $E_n = 0 \dots 20 \text{ MeV}$
- Good agreement with both preliminary experimental results and model calculations for
 - $E_{\gamma,tot}(E_n)$
 - $\epsilon_{\gamma}(E_n)$
 - $v_{\gamma}(E_n)$













- ${}^{235}U(n, f)$ at $E_n = 1.5$ MeV, LICORNE (2013)
 - 14 BaF₂ detectors
 - 3 LaBr₃:Ce detectors (1 week)







- 235 U(n, f) at E_n = 1.5 MeV, LICORNE (2013)
 - 14 BaF₂ detectors
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- 235 U(n, f) at E_n = 1.5 MeV, LICORNE (2013)
 - 14 BaF₂ detectors
 - 3 LaBr₃:Ce detectors (1 week) –
- $\begin{array}{l} \mbox{preliminary:} \\ E_{\gamma,tot} = (7.4 \pm 0.7) \mbox{ MeV} \\ \overline{v}_{\gamma} &= (8.7 \pm 0.4) \\ \epsilon_{\gamma} &= (0.85 \pm 0.07) \mbox{ MeV} \end{array}$







- 235 U(n, f) at $E_n = 1.5$ MeV, LICORNE (2013)
 - 14 BaF₂ detectors
 - 3 LaBr₃:Ce detectors (1 week) –

Predictions! <---

 $\begin{array}{c} \text{preliminary:} \\ E_{\gamma,\text{tot}} = (7.4 \pm 0.7) \text{ MeV} \\ \overline{v}_{\gamma} = (8.7 \pm 0.4) \\ \epsilon_{\gamma} = (0.85 \pm 0.07) \text{ MeV} \end{array}$





Average total energy per fission



- Tudora et al.: Phys. Procedia 31 (2012)
- LICORNE: preliminary results (2014)
- DANCE: Chyzh et al. (2013) and (2014)







- LICORNE: preliminary results (2014)
- DANCE: Chyzh et al. (2013) and (2014)







Mean energy per photon



- LICORNE: preliminary results (2014)
- DANCE: Chyzh et al. (2013) and (2014)





Recently ...

- 235 U(n, f) at E_n = 1.5 MeV, LICORNE (2013)
 - 14 BaF₂ detectors
 - 3 LaBr₃:Ce detectors (1 week) –
- preliminary: $E_{\gamma,tot} = (7.4 \pm 0.7) \text{ MeV}$ $\overline{v}_{\gamma} = (8.7 \pm 0.4)$ $\epsilon_{\gamma} = (0.85 \pm 0.07) \text{ MeV}$
- ^{240,242}Pu(sf), IRMM (on-going)
 - 1 LaBr₃:Ce detector (1 week)













Recently ...

- ${}^{235}U(n, f)$ at $E_n = 1.5$ MeV, LICORNE (2013)
 - 14 BaF₂ detectors
 - 3 LaBr₃:Ce detectors (1 week) –

- ^{240,242}Pu(sf), IRMM (on-going)
 - 1 LaBr₃:Ce detector (1 week) –
 ²⁴⁰Pu(sf)
 - $E_{\gamma,tot} = (6.9\pm0.7) \text{ MeV}$ $\overline{v}_{\gamma} = (7.7\pm0.5)$
 - $\overline{\mathbf{v}}_{\gamma} =$ $\varepsilon_{\gamma} =$
- (0.9±0.1) MeV

- preliminary: $E_{\gamma,tot} = (7.4\pm0.7) \text{ MeV}$ $\overline{v}_{\gamma} = (8.7\pm0.4)$ $\epsilon_{\gamma} = (0.85\pm0.07) \text{ MeV}$
- preliminary: ²⁴²Pu(sf) (6.9±0.3) MeV (7.7±0.4) (0.89±0.06) MeV



New evaluation PFGS average total energy per fission



Observe: \overline{v}_n taken from ENDF/B-VII.1.

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New evaluation PFGS mean energy per photon





New evaluation PFGS average multiplicity





Observe: \overline{v}_n taken from ENDF/B-VII.1.







- ${}^{235}U(n, f)$ at $E_n = 1.5$ MeV, LICORNE (2013)
 - 14 BaF₂ detectors
 - 3 LaBr₃:Ce detectors (1 week) preliminary:
 - $\begin{array}{l} {\sf E}_{\gamma,tot} = (7.4 {\pm} 0.7) \; {\sf MeV} \\ \overline{{\sf v}}_{\gamma} &= (8.7 {\pm} 0.4) \\ \epsilon_{\gamma} &= (0.85 {\pm} 0.07) \; {\sf MeV} \end{array}$
- ^{240,242}Pu(sf), IRMM (on-going)
 - 1 LaBr₃:Ce detector (1 week) –
 ²⁴⁰Pu(sf)
 - $E_{\gamma,tot} = (6.9\pm0.7) \text{ MeV}$ $\overline{v}_{\gamma} = (7.7\pm0.5)$ $\varepsilon_{\gamma} = (0.9\pm0.1) \text{ MeV}$
- preliminary: ²⁴²Pu(sf) (6.9±0.3) MeV (7.7±0.4) (0.89±0.06) MeV
- ²³⁵U,^{239,241}Pu(n, f) and ²⁵²Cf(sf), DANCE (2014)
 - 160 BaF₂ detectors

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Conclusions



- Systematics of PFGS characteristics as function of A and Z of the compound system makes sense, <u>not only for thermal neutron induced and</u> spontaneous fission
- Original parameters from Valentine's description need an adjustment
- Empirical A and Z dependence must be verified
- More experimental data needed
- Predictions for fast neutron induced fission of $n + {}^{238}U$ and $n + {}^{235}U$ presented
- Good agreement of our predictions with both calculations and preliminary experimental results!







- From LICORNE experiment ($E_n = 1.5 \text{ MeV}$):
 - final analysis of PFGS for ^{235,238}U(n, f) and ²³²Th(n, f)
- Laborie et al.:
 - final analysis of PFGS for ²³⁸U(n, f)
- IRMM:
 - final analysis of PFGS for ^{240,242}Pu(sf)
- New experiment at KFKI Budapest:
 - PFGS from ²³⁹Pu(n_{th}, f) spring 2015 (planned)
- New experiment with LICORNE at IPN Orsay:
 - PFGS from ²³⁹Pu(n, f) summer 2015 (planned)
- Updated systematics!
- New predictions!



The collaborators



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Thank you!



NEUTRON PRODUCTION IN INVERSE KINEMATICS

mercredi 2 octobre 2013



Lithium Inverse Cinematiques ORsay NEutron source

> p(⁷Li,⁷Be)n reaction in inverse kinematics

INSTITUT DE PHYSIQUE NUCLÉAIRE ORSAY

MONO-ENERGETIC NEUTRON SOURCES

mercredi 2 octobre 2013



>Typically over 99% of neutrons 'wasted"

>Wasted neutrons contribute to the room background

> Placement of gamma detectors impossible without heavy shielding





EXPERIMENTAL SETUP: MEASUREMENT OF PROMPT γ FOR FISSILE NUCLEI (JULY 2013)

LaBr₃ from IPN & IRMM ($\delta t = 300 \text{ ps}; \delta E = <3\% @ .662 \text{ MeV}$)



BaF₂ from Château de Cristal (δt = 600 ps; δE = 10% @ 1.3 MeV) **Ionisation Chamber** ²³⁵⁻²³⁸U target 10 mg (300 μg/cm²); Ø = 8 cm; (δt = 700 ps; δE = 500 keV; ε = 100%)

BaF₂ from Château de Cristal (δt = 600 ps; δE = 10% @ 1.3 MeV)











Measured ²⁵²Cf(sf) prompt fission γ -ray energy spectrum \rightarrow e.g. zooming into region around 3 MeV

Theory-2, Biarritz (France), November 28-30, 2012



Unfolding response function (an illustration)





Simulating response function for mono-energetic γ-rays, distance: FWHM from energy resolution measurements







Adjusting simulated spectra to measured γ-ray spectrum and determining the scaling factors







Properly normalized scaling factors

 \rightarrow emission spectrum!





Fast neutron induced fission Prerequisites

According to Valentine:

- $E_{\gamma,tot}$ depending linearly on \overline{v}_n , ε_{γ} independent
- $\overline{\mathbf{v}}_{\gamma}$ approximately proportional to $\overline{\mathbf{v}}_{n}$
- Knowledge of $\overline{v}_n(E_n)$ important

In case of multiple chance fission:

- (n, f) cross section has to be known (ENDF/B-VII.1)
- Contributions from different fission channels have to be taken into account
- $\overline{v}_n(E_n)$ for all fissioning systems (ENDF/B-VII.1)





ENDB/B-VII.1



Contributions from different fission channels.




ENDB/B-VII.1





²³⁸U(n, f) PFGS characteristics Prompt fission neutron multiplicity



Chen & Liu:

prompt fission neutrons =
evaporation neutrons (pre-fission) +
prompt neutrons from fission fragments!



²³⁸U(n, f) PFGS characteristics Prompt fission neutron multiplicity



Chen & Liu:

prompt fission neutrons =
evaporation neutrons (pre-fission) +
prompt neutrons from fission fragments!
only the latter may be related to PFGS!

Claim:

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Energetics:

$$\begin{split} E_{x}^{A_{CN}} &= S_{n}^{A_{CN}} + E_{n}; \qquad \left\langle E_{n} \right\rangle = \frac{3}{2}T = \frac{3}{2}\sqrt{\frac{7.524MeV \cdot E_{x}^{A_{CN}}}{A_{CN}}} \quad *) \\ E_{x}^{A_{CN}-1} &= S_{n}^{A_{CN}-1} + E_{n}^{'} = E_{x}^{A_{CN}} - S_{n}^{A_{CN}} - \left\langle E_{n} \right\rangle; \qquad \left\langle E_{n}^{'} \right\rangle = \frac{3}{2}T^{'} = \frac{3}{2}\sqrt{\frac{7.524MeV \cdot E_{x}^{A_{CN}-1}}{A_{CN}-1}} \\ E_{x}^{A_{CN}-2} &= S_{n}^{A_{CN}-2} + E_{n}^{''} = E_{x}^{A_{CN}-1} - S_{n}^{A_{CN}-1} - \left\langle E_{n}^{'} \right\rangle; \qquad \left\langle E_{n}^{''} \right\rangle = \frac{3}{2}T^{''} = \frac{3}{2}\sqrt{\frac{7.524MeV \cdot E_{x}^{A_{CN}-1}}{A_{CN}-1}} \\ etc. \end{split}$$

*) According to Chen & Liu: $E_x^{A_{CN}} = \frac{A_{CN}}{7.524 MeV} T^2$

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²³⁸U(n, f) PFGS characteristics



Prompt fission neutron multiplicity



- prompt fission neutrons from ENDF/B-VII.1
- pre-fission neutrons subtracted
- prompt neutrons from fragments for PFGS characteristics