

A new approach to fission dynamics

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More details in [Bertsch, arXiv:1407.1899.pdf](#)

## Why a new approach?

- Incorporate diffusive dynamics in the computational framework.  
J. Randrup and P. Moller, Phys. Rev. Lett. 106 12305
- Computations are easier in discrete bases and implementation of continuum approaches rely on discrete configurations.  
R. Bernard, H. Goutte, D. Gogny, and W. Younes, Phys, Rev. C 84 044308
- There is data that is incompatible with the present computational approach.

U-235+n ---> fission;  $E_B = 5.67$  MeV,  $S_n = 6.55$  MeV  
Moore, et al., Phys. Rev. C18 1328 (1978)  
Moore, et al., Phys. Rev. C30, 214 (1980)

1346

MOORE, MOSES, KEYWORTH, DABBS, AND HILL

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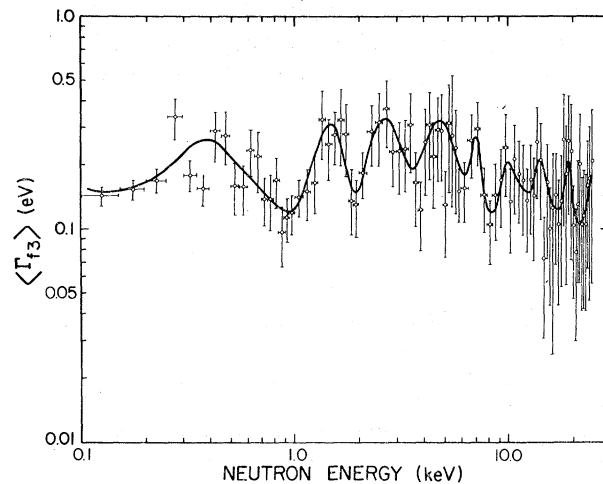


FIG. 16. Average spin-3 fission width for  $(^{235}\text{U}+n)$  from 0.1 to 25 keV obtained from the unresolved resonance analysis described in the text. The curve has no theoretical significance; it is simply the authors' eyeguide.

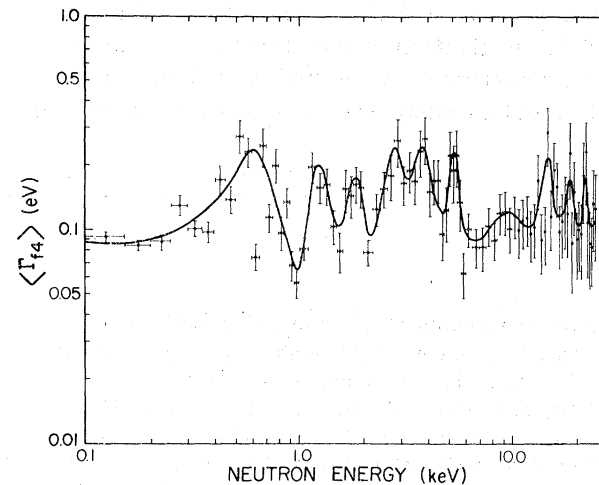
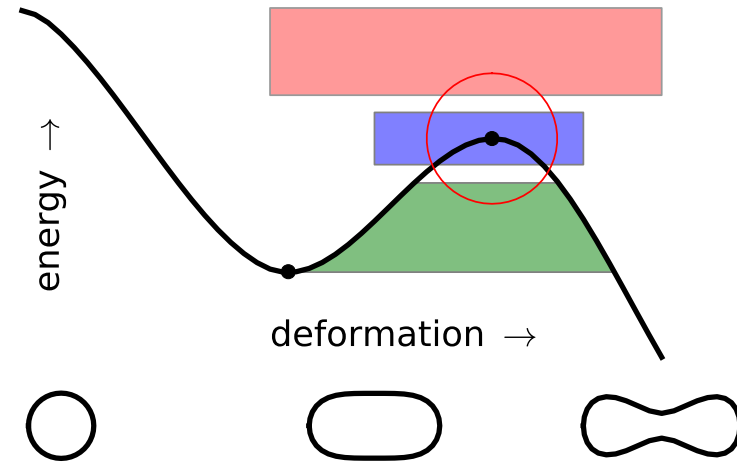
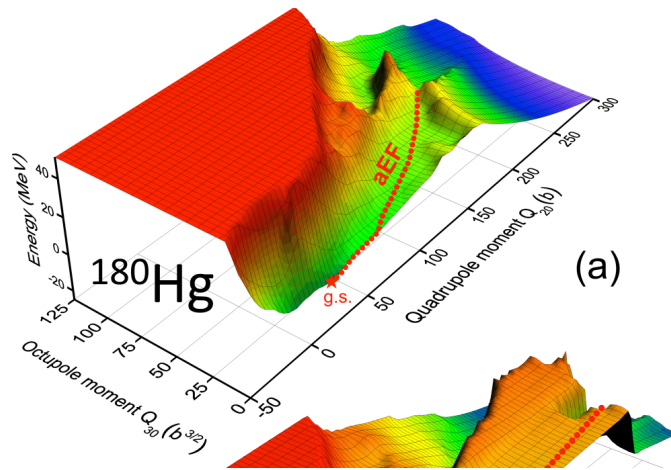


FIG. 17. Average spin-4 fission width for  $(^{235}\text{U}+n)$  from 0.1 to 25 keV obtained from the unresolved resonance analysis described in the text. The curve has no theoretical significance; it is simply the authors' eyeguide.

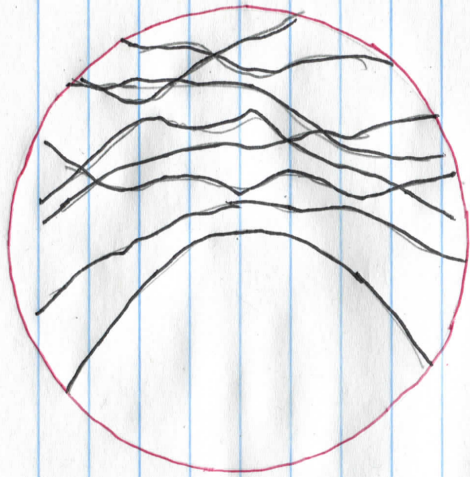
# The landscape

PHYSICAL REVIEW C **90**, 021302(R) (2014)

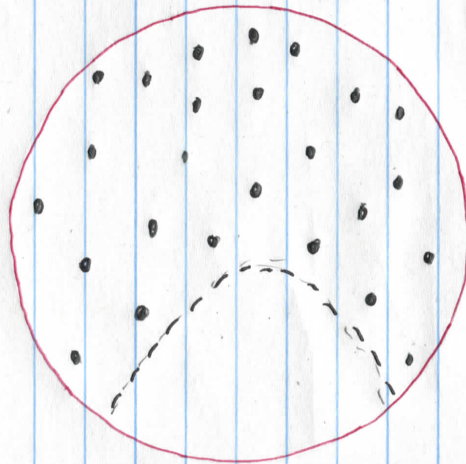


# Choice of representation

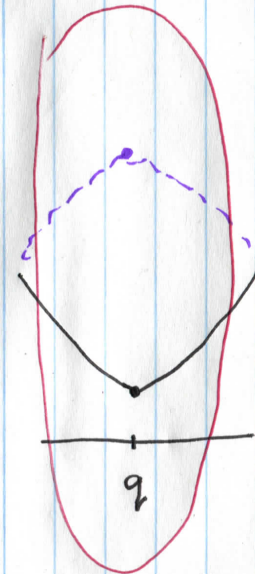
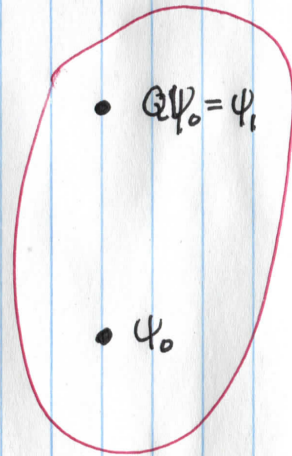
GCM representation



Discrete-basis representation



The two representations are equivalent,  
in principle



$$\Psi(q) \sim \sqrt{1-q^2} \Psi_0 + q \Psi_1$$

## The Hamiltonian

Level density:

Definition

$$\rho(q, E) = \sum_i \delta(q - q_i) \delta(E - E_i).$$

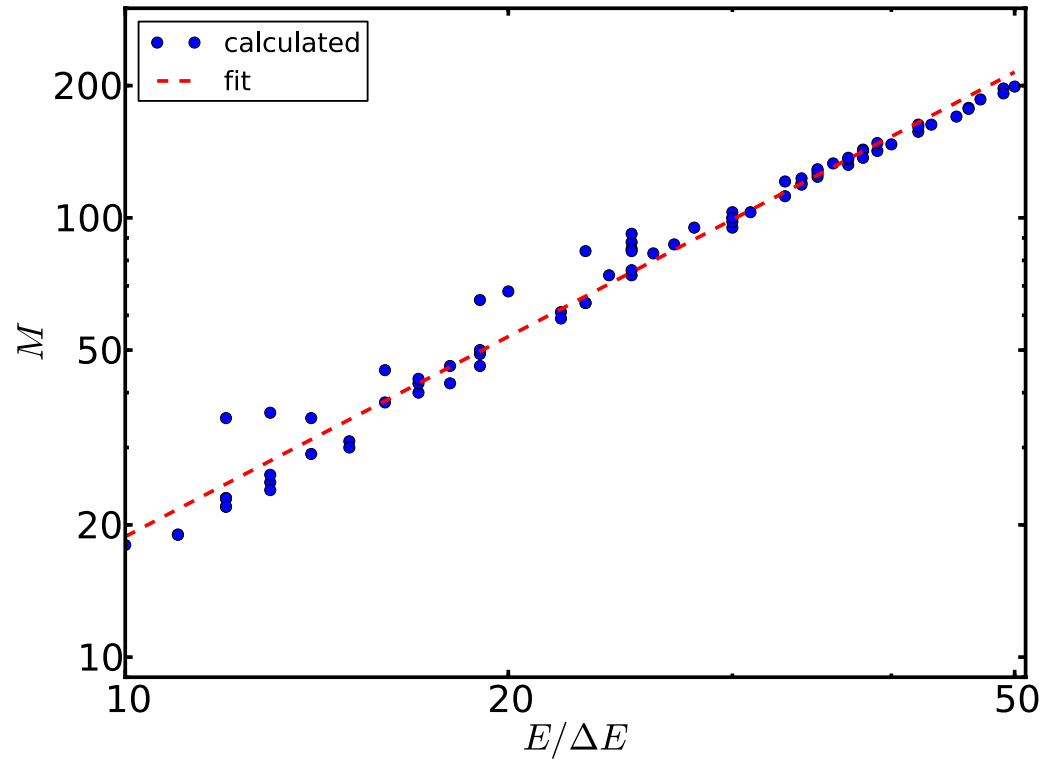
Parameterization

$$\rho(q, E) = \rho_0 \exp(\beta(E - V_0(q))).$$

Off-diagonal interaction:

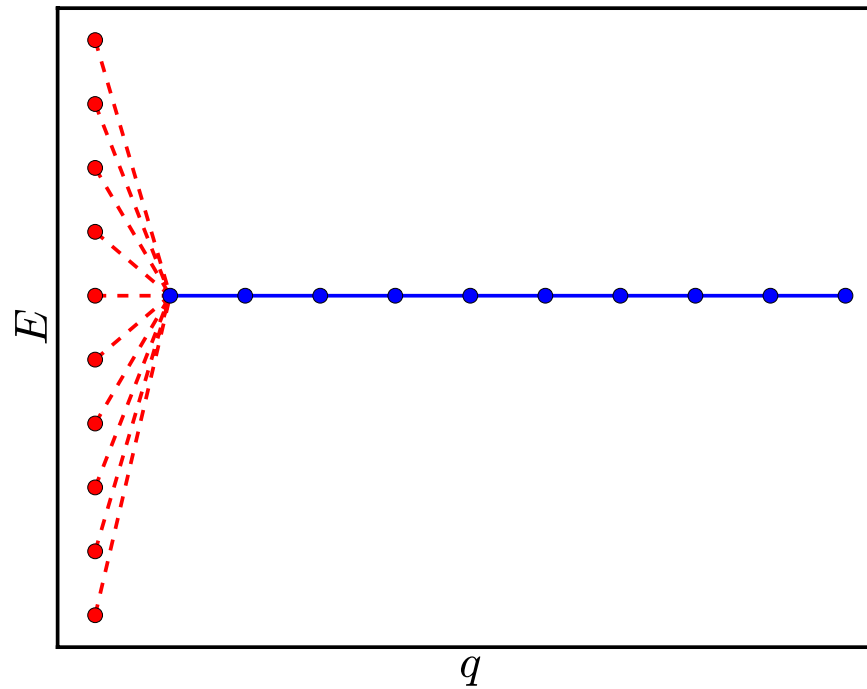
$$\overline{\langle i|v|j\rangle^2} = v_0^2 e^{-(q_i - q_j)^2 / 2q_0^2} \frac{(E_i + E_j)^{3/2}}{(\rho(E_i)\rho(E_j))^{1/2}}$$

### Fit to a power law



$$M \sim E^{**1.51}$$

## Channel physics in the discrete basis



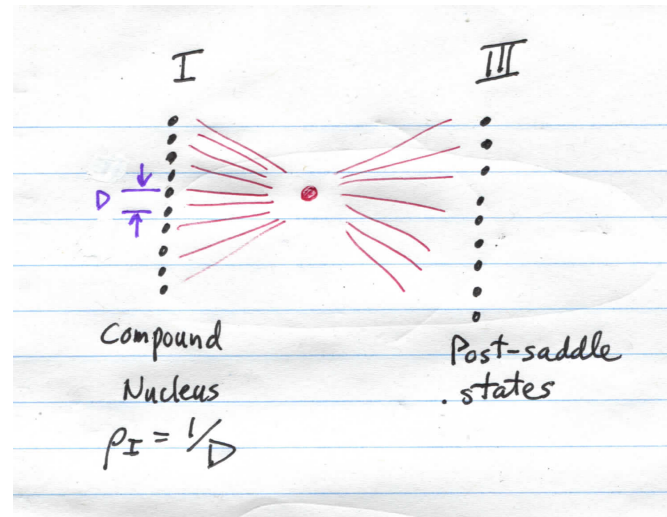
Red dots: compound nucleus states  
Blue dots: channel states



Where is the point of no return?

R-matrix answer: at the top of the outer barrier

My answer: when the local level density exceeds  $\rho_I$



Verified by numerical experiments.

When does the dynamics become diffusive?

$$\frac{\partial P}{\partial t} = D \frac{\partial^2 P}{\partial q^2}. \quad (1)$$

The diffusion coefficient  $D$  is given by

$$D(q_i, E_i) = 2\pi\hbar \sum_j (q_i - q_j)^2 \langle i|v|j\rangle^2 \delta(E_i - E_j) \quad (2)$$

The control parameter determining the proximity to the diffusive limit is

$$\alpha = q_0 \rho_0 v_0 \quad (3)$$

See B.W. Bush, G.F. Bertsch, and B.A. Brown, Phys. Rev. C 45 1709 (1992)

## Connection to mesoscopic physics

### The Landauer formula for conductance

$$C = R^{-1} = \frac{e^2}{2\pi\hbar} \sum_c T_c$$

Derived from the Bohr-Wheeler formula:  
J. Phys. Cond. Mat. **3** 373 (1991)

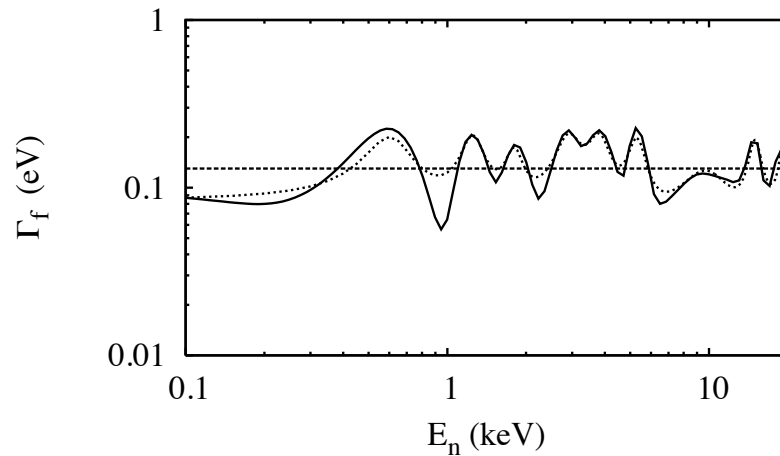
$$W = \frac{1}{2\pi\hbar\rho_I} \sum_c T_c.$$

### Quantum-dot-mediated conductance

$$\sum_c T_c \rightarrow \sum_b \frac{\Gamma_{bR}\Gamma_{bL}}{E_b^2 + (\Gamma_{bR} + \Gamma_{bL})^2/4}$$

## A challenge to R-matrix theory

U-235+n ---> fission;  $E_B = 5.67$  MeV,  $S_n = 6.55$  MeV



Solid line: experiment from Moore, et al., PRC 30 214 (1984).

How can one get fluctuations on the scale of 1 keV at 1 MeV above the barrier?  
Dashed line: a fit with 13 non-interfering resonances.

$$W = \frac{1}{2\pi\hbar\rho_I} \sum_c T_c. \quad \sum_c T_c \rightarrow \sum_b \frac{\Gamma_{bR}\Gamma_{bL}}{E_b^2 + (\Gamma_{bR} + \Gamma_{bL})^2/4}$$

R-matrix theory requires a parameterization

$$\sum_c T_c = \sum_c \frac{1}{1 + \exp(2\pi(E_c - E)/\hbar\omega)}$$

Details (Bouland, Lynn, Talou, Phys. Rev. C88 054612)

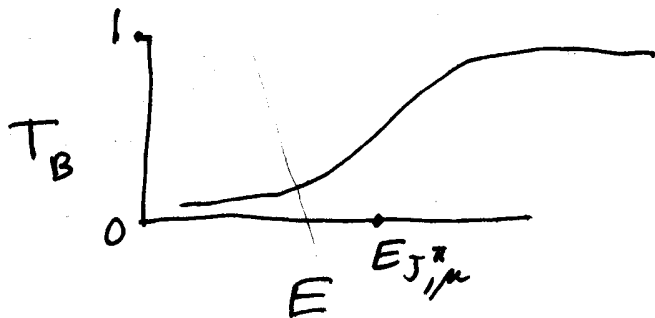
$$\sigma_{nf}(E, J^\pi) = \sigma_n(E, J^\pi) P_f(E, J^\pi)$$

$$P_f = \frac{\sum T_f}{\sum T_f + T_{I,y} + T_{I,n}}$$

$$\Gamma_f = \frac{1}{2\pi\rho_I} P_f$$

$$T_f = \frac{T_A T_B}{T_A + T_B + T_{II,y} + T_{II,n}}$$

$$T_B(E, J_{,\mu}^\pi) = \frac{1}{1 + \exp(2\pi(E_{J_{,\mu}^\pi} - E)/\hbar\omega)}$$



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